

Lecture 8 of 41

Scan Conversion 2 of 2: Circles/Ellipses and Polygons

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KSOL course pages: <http://bit.ly/hGvXIH> / <http://bit.ly/eVizrE>

Public mirror web site: <http://www.kddresearch.org/Courses/CIS636>

Instructor home page: <http://www.cis.ksu.edu/~bhsu>

Readings:

Today: Sections 2.4, 2.5 esp. 2.5.4, 3.1.6, Eberly 2^e – see <http://bit.ly/ieUq45>

Next class: Sections 2.5, 2.6.1-2.6.2, 4.3.2, 20.2, Eberly 2^e

Brown CS123: Scan Conversion (<http://bit.ly/hfbF0D>), Shapes
(<http://bit.ly/hatPSi>), Polygons/Texture Mapping (<http://bit.ly/h2VZn8>)

Wayback Machine archive of Brown CS123 slides: <http://bit.ly/gAhJbh>

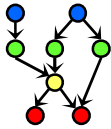




Lecture Outline

- **Readings**
 - * Last class: §2.3.5, 2.4, 3.1.3, Eberly 2^e
 - * Today's class: §2.4, 2.5 (Especially 2.5.4), 3.1.6, Eberly 2^e
 - * Next class: §2.5, 2.6.1-2.6.2, 4.3.2, 20.2, Eberly 2^e
- **Excerpts from Van Dam notes, Brown CS123**
 - * Scan converting circles/ellipses (starting from 19 in fall, 2010 notes)
 - * Polygons (Shapes 2-4)
 - * Triangle meshes (Shapes 13-14)
 - * Scan line interpolation (Polygons 7; Shading 14, 2005 – 2009 notes)
- **Last Time: Intro to Clipping and Culling**
 - * Clipping: Cohen-Sutherland, Cyrus-Beck / Liang-Barsky
 - * Visibility Culling: view frustum, back face, occlusion
- **Today: Scan Conversion, Concluded**
 - * Circles and ellipses
 - * Polygons





Where We Are

Lecture	Topic	Primary Source(s)
0	Course Overview	Chapter 1, Eberly 2 ^e
1	CG Basics: Transformation Matrices; Lab 0	Sections (§) 2.1, 2.2
2	Viewing 1: Overview, Projections	§ 2.2.3 – 2.2.4, 2.8
3	Viewing 2: Viewing Transformation	§ 2.3 esp. 2.3.4; FVFH slides
4	Lab 1a: Flash & OpenGL Basics	Ch. 2, 16¹, Angel Primer
5	Viewing 3: Graphics Pipeline	§ 2.3 esp. 2.3.7; 2.6, 2.7
6	Scan Conversion 1: Lines, Midpoint Algorithm	§ 2.5.1, 3.1; FVFH slides
7	Viewing 4: Clipping & Culling; Lab 1b	§ 2.3.5, 2.4, 3.1.3
8	Scan Conversion 2: Polygons, Clipping Intro	§ 2.4, 2.5 esp. 2.5.4, 3.1.6
9	Surface Detail 1: Illumination & Shading	§ 2.5, 2.6.1 – 2.6.2, 4.3.2, 20.2
10	Lab 2a: Direct3D / DirectX Intro	§ 2.7, Direct3D handout
11	Surface Detail 2: Textures; OpenGL Shading	§ 2.6.3, 20.3 – 20.4, Primer
12	Surface Detail 3: Mappings; OpenGL Textures	§ 20.5 – 20.13
13	Surface Detail 4: Pixel/Vertex Shad.; Lab 2b	§ 3.1
14	Surface Detail 5: Direct3D Shading; OGLSL	§ 3.2 – 3.4, Direct3D handout
15	Demos 1: CGA, Fun; Scene Graphs: State	§ 4.1 – 4.3, CGA handout
16	Lab 3a: Shading & Transparency	§ 2.6, 20.1, Primer
17	Animation 1: Basics, Keyframes; HW/Exam	§ 5.1 – 5.2
	Exam 1 review; Hour Exam 1 (evening)	Chapters 1 – 4, 20
18	Scene Graphs: Rendering; Lab 3b: Shader	§ 4.4 – 4.7
19	Demos 2: SFX; Skinning, Morphing	§ 5.3 – 5.5, CGA handout
20	Demos 3: Surfaces; B-reps/Volume Graphics	§ 10.4, 12.7, Mesh handout

Lightly-shaded entries denote the due date of a written problem set; heavily-shaded entries, that of a machine problem (programming assignment); blue-shaded entries, that of a paper review, and the green-shaded entry, that of the term project.

Green, blue and red letters denote exam review, exam, and exam solution review dates.





Drawing Circles, Versions 1 & 2

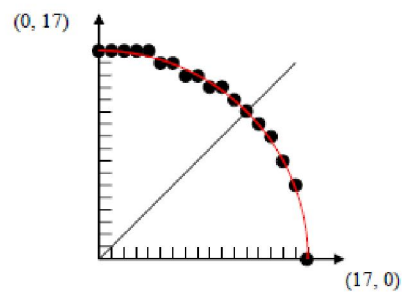
Version 1: really bad

For x from $-R$ to R :

$$y = \sqrt{R * R - x * x};$$

Pixel (round(x), round(y));

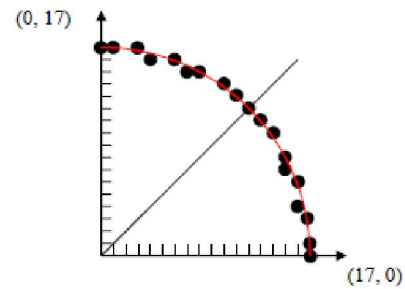
Pixel (round(x), round($-y$));



Version 2: slightly less bad

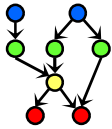
For x from 0 to 360:

Pixel (round ($R * \cos(x)$),
round ($R * \sin(x)$));



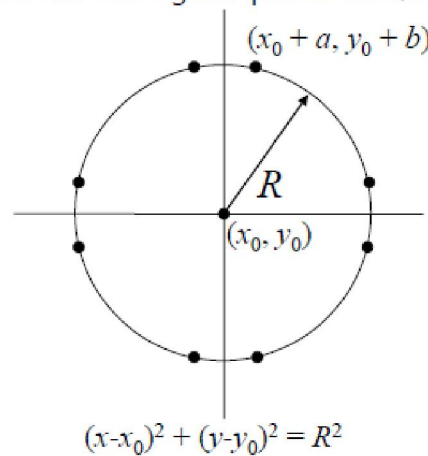
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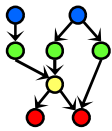
Drawing Circles, Version 3

- Symmetry: If $(x_0 + a, y_0 + b)$ is on circle
 - also $(x_0 \pm a, y_0 \pm b)$ and $(x_0 \pm b, y_0 \pm a)$, hence 8-way symmetry.
- Reduce the problem to finding the pixels for 1/8 of the circle



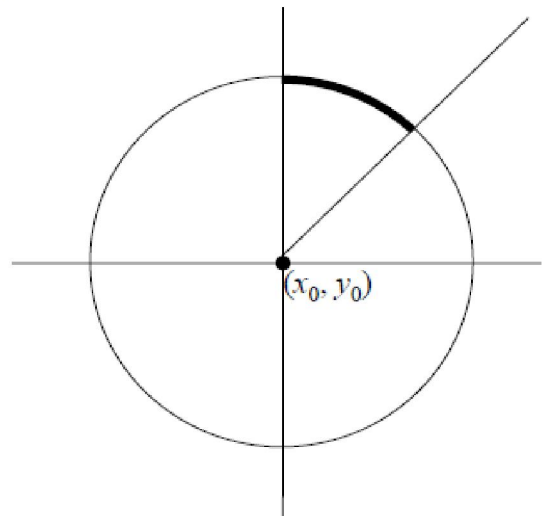
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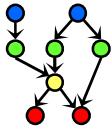
Using The Symmetry

- ▶ Scan top right 1/8 of circle of radius R
- ▶ Circle starts at $(x_0, y_0 + R)$
- ▶ Let's use another incremental algorithm with decision variable evaluated at midpoint



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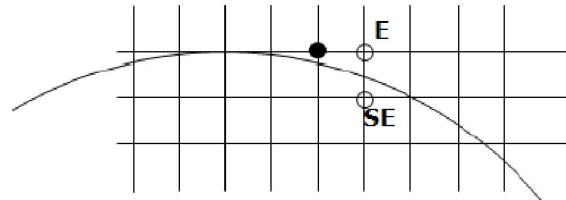


Incremental Algorithm [1]: Sketch

```

x = x0, y = y0 + R, Pixel(x, y);
for (x = x0 + 1; (x - x0) > (y - y0); x++) {
  if (decision var < 0) {
    /* move east */
    update decision variable
  }
  else {
    /* move south east */
    update decision variable
    y--;
  }
  Pixel(x, y);
}

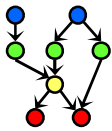
```



- ▶ Note: can replace all occurrences of x_0, y_0 with 0, shifting coordinates by $(-x_0, -y_0)$

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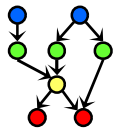


Incremental Algorithm [2]: Computations needed

- ▶ Decision variable
 - ▶ negative if we move E, positive if we move SE (or vice versa).
- ▶ Follow line strategy: Use implicit equation of circle
 - ▶ $f(x, y) = x^2 + y^2 - R^2 = 0$
 - ▶ $f(x, y)$ is zero on circle, negative inside, positive outside
- ▶ If we are at pixel (x, y) examine $(x + 1, y)$ and $(x + 1, y - 1)$
- ▶ Compute f at the midpoint

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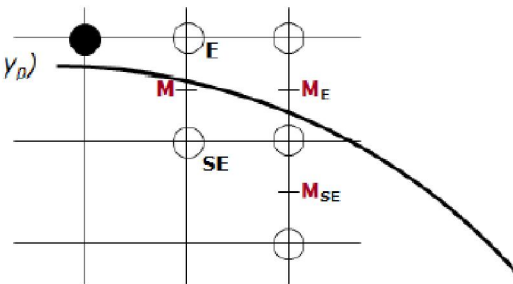


Decision Variable

- ▶ Evaluate $f(x, y) = x^2 + y^2 - R^2$ at the point:

$$\left(x+1, y-\frac{1}{2}\right)$$

$P = (x_D, y_D)$



- ▶ We are asking: “Is

$$f\left(x+1, y-\frac{1}{2}\right) = (x+1)^2 + \left(y-\frac{1}{2}\right)^2 - R^2$$

positive or negative?” (it is zero on circle)

- ▶ If **negative**, midpoint inside circle, **choose E**
 - ▶ *vertical* distance to the circle is less at $(x + 1, y)$ than at $(x + 1, y - 1)$
- ▶ If **positive**, opposite is true, **choose SE**

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Right Decision Variable?

- ▶ Decision based on vertical distance
- ▶ Ok for lines, since d and d_{vert} are proportional
- ▶ For circles, not true:

$$d((x + 1, y), Circ) = \sqrt{(x + 1)^2 + y^2} - R$$

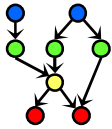
$$d((x + 1, y - 1), Circ) = \sqrt{(x + 1)^2 + (y - 1)^2} - R$$

- ▶ Which d is closer to zero? (i.e. which of the two values below is closer to R):

$$\sqrt{(x + 1)^2 + y^2} \text{ or } \sqrt{(x + 1)^2 + (y - 1)^2}$$

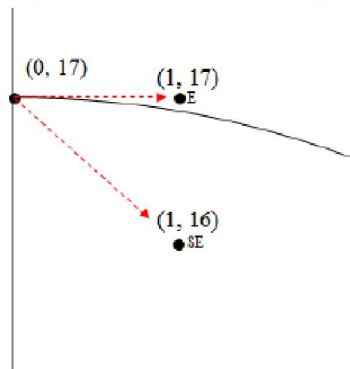
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Alternate Phrasing [1]

- ▶ We could ask instead:
“Is $(x + 1)^2 + y^2$ or $(x + 1)^2 + (y - 1)^2$ closer to R^2 ?”
- ▶ The two values in equation above differ by
- ▶ $[(x + 1)^2 + y^2] - [(x + 1)^2 + (y - 1)^2] = 2y - 1$



$$f_E = 1^2 + 17^2 = 290$$

$$f_{SE} = 1^2 + 16^2 = 257$$

$$f_E - f_{SE} = 290 - 257 = 33$$

$$2y - 1 = 2(17) - 1 = 33$$

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Alternate Phrasing [2]

- ▶ The second value, which is always less, is *closer* if its difference from R^2 is less than: $\frac{1}{2}(2y - 1)$

$$\text{i.e., if } R^2 - [(x + 1)^2 + (y - 1)^2] < \frac{1}{2}(2y - 1)$$

$$\text{then } 0 < y - \frac{1}{2} + (x + 1)^2 + (y - 1)^2 - R^2$$

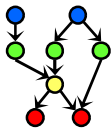
$$0 < (x + 1)^2 + y^2 - 2y + 1 + y - \frac{1}{2} - R^2$$

$$0 < (x + 1)^2 + y^2 - y + \frac{1}{2} - R^2$$

$$0 < (x + 1)^2 + (y - \frac{1}{2})^2 + \frac{1}{4} - R^2$$

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Alternate Phrasing [3]

- ▶ The **radial distance decision** is whether

$$d_1 = (x + 1)^2 + \left(y - \frac{1}{2}\right)^2 + \frac{1}{4} - R^2$$

is positive or negative.

- ▶ The **vertical distance decision** is whether

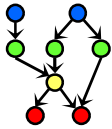
$$d_2 = (x + 1)^2 + \left(y - \frac{1}{2}\right)^2 - R^2$$

is positive or negative; d_1 and d_2 are $\frac{1}{4}$ apart.

- ▶ The integer d_1 is positive only if $d_2 + \frac{1}{4}$ is positive (except special case where $d_2 = 0$: remember you're using integers).

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Incremental Algorithm Revisited [1]

- ▶ How to compute the value of

$$f(x, y) = (x + 1)^2 + \left(y - \frac{1}{2}\right)^2 - R^2$$

at successive points? (vertical distance approach)

- ▶ Answer: Note that $f(x + 1, y) - f(x, y)$

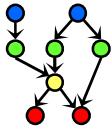
is $\Delta_E(x, y) = 2x + 3$

and that $f(x + 1, y - 1) - f(x, y)$

is just $\Delta_{SE}(x, y) = 2x + 3 - 2y + 2$

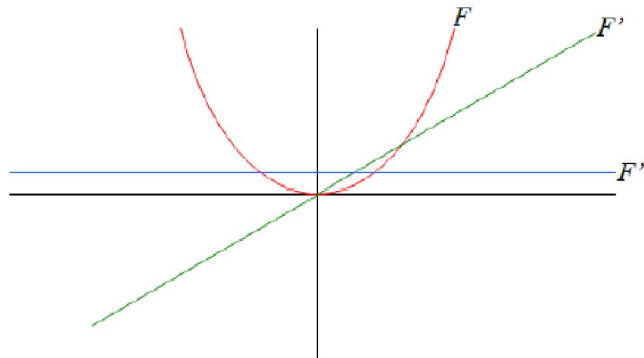
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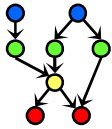
Incremental Algorithm Revisited [2]

- ▶ If we move E, update by adding $2x + 3$
- ▶ If we move SE, update by adding $2x + 3 - 2y + 2$
- ▶ Forward differences of a 1st degree polynomial are constants and those of a 2nd degree polynomial are 1st degree polynomials
 - ▶ this “first order forward difference,” like a partial derivative, is one degree lower



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Second Differences [1]

- ▶ The function $\Delta_E(x, y) = 2x + 3$ is linear, hence amenable to incremental computation:

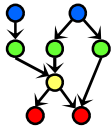
$$\begin{aligned}\Delta_E(x + 1, y) - \Delta_E(x, y) &= 2 \\ \Delta_E(x + 1, y - 1) - \Delta_E(x, y) &= 2\end{aligned}$$

- ▶ Similarly

$$\begin{aligned}\Delta_{SE}(x + 1, y) - \Delta_{SE}(x, y) &= 2 \\ \Delta_{SE}(x + 1, y - 1) - \Delta_{SE}(x, y) &= 4\end{aligned}$$

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Second Differences [2]

- ▶ For any step, can compute new $\Delta_E(x, y)$ from old $\Delta_E(x, y)$ by adding appropriate second constant increment – update delta terms as we move.
 - ▶ This is also true of $\Delta_{SE}(x, y)$
- ▶ Having drawn pixel (a, b) , decide location of new pixel at $(a + 1, b)$ or $(a + 1, b - 1)$, using previously computed $\Delta(a, b)$
- ▶ Having drawn new pixel, must update $\Delta(a, b)$ for next iteration; need to find either $\Delta(a + 1, b)$ or $\Delta(a + 1, b - 1)$ depending on pixel choice
- ▶ Must add $\Delta_E(a, b)$ or $\Delta_{SE}(a, b)$ to $\Delta(a, b)$
- ▶ So we...
 - ▶ Look at d to decide which to draw next, update x and y
 - ▶ Update d using $\Delta_E(a, b)$ or $\Delta_{SE}(a, b)$
 - ▶ Update each of $\Delta_E(a, b)$ and $\Delta_{SE}(a, b)$ for future use
 - ▶ Draw pixel

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Midpoint Eighth Circle Algorithm

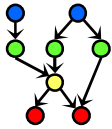
```

MEC (R) /* 1/8th of a circle w/ radius R */ {
    int    x = 0, y = R;
    int    delta_E    = 2*x + 3;
    int    delta_SE   = 2(x-y) + 5;
    float  decision   = (x+1)*(x+1) + (y + 0.5)*(y + 0.5) - R*R;
    Pixel(x, y);
    while( y > x ) {
        if (decision > 0) /* Move east */
            decision += delta_E;
            delta_E += 2; delta_SE += 2; /*Update delta*/
        else /* Move SE */ {
            y--;
            decision += delta_SE;
            delta_E += 2; delta_SE += 4; /*Update delta*/
        }
        x++; Pixel(x, y); }
}

```

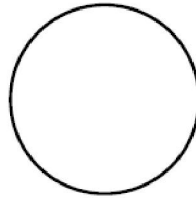
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Analysis

- ▶ Uses floats!
- ▶ 1 test, 3 or 4 additions per pixel
- ▶ Initialization can be improved
- ▶ Multiply everything by 4: No Floats!
 - ▶ Makes the components even, but sign of decision variable remains same



Questions

- ▶ Are we getting all pixels whose distance from the circle is less than $\frac{1}{2}$?
- ▶ Why is $y > x$ the right stopping criterion?
- ▶ What if it were an ellipse?

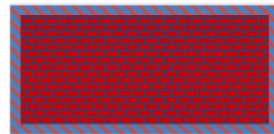
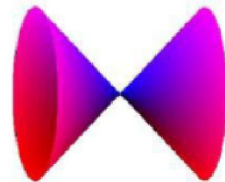
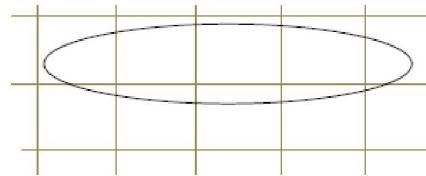
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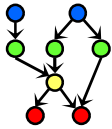
Other Scan Conversion Problems

- ▶ Aligned Ellipses
- ▶ Non-integer primitives
- ▶ General conics
- ▶ Patterned primitives



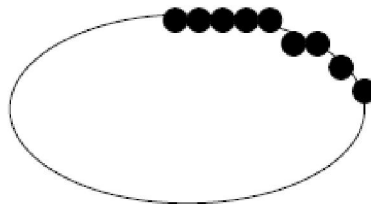
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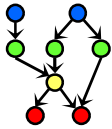
Aligned Ellipses

- ▶ Equation is $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ i.e, $b^2x^2 + a^2y^2 = a^2b^2$
- ▶ Computation of Δ_E and Δ_{SE} is similar
- ▶ Only 4-fold symmetry
- ▶ When do we stop stepping horizontally and switch to vertical?



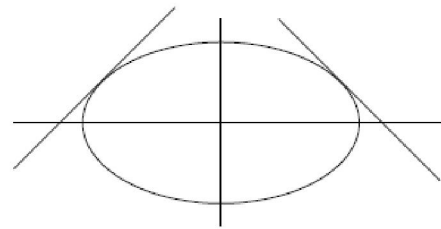
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Direction-Changing Criterion [1]

- ▶ When absolute value of slope of ellipse is more than 1:



- ▶ How do you check this? At a point (x, y) for which $f(x, y) = 0$, a vector perpendicular to the level set is $\nabla f(x, y)$ which is

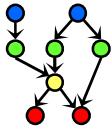
$$\left[\frac{\partial f}{\partial x}(x, y), \frac{\partial f}{\partial y}(x, y) \right]$$

- ▶ This vector points more right than up when

$$\frac{\partial f}{\partial x}(x, y) - \frac{\partial f}{\partial y}(x, y) > 0$$

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Direction-Changing Criterion [2]

- ▶ In our case, $\frac{\partial f}{\partial x}(x, y) = 2a^2x$ and $\frac{\partial f}{\partial y}(x, y) = 2b^2y$

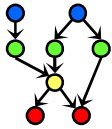
so we check for

$$2a^2x - 2b^2y > 0$$
$$a^2x - b^2y > 0$$

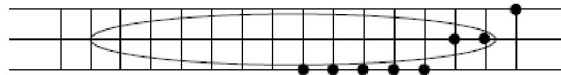
- ▶ This, too, can be computed incrementally

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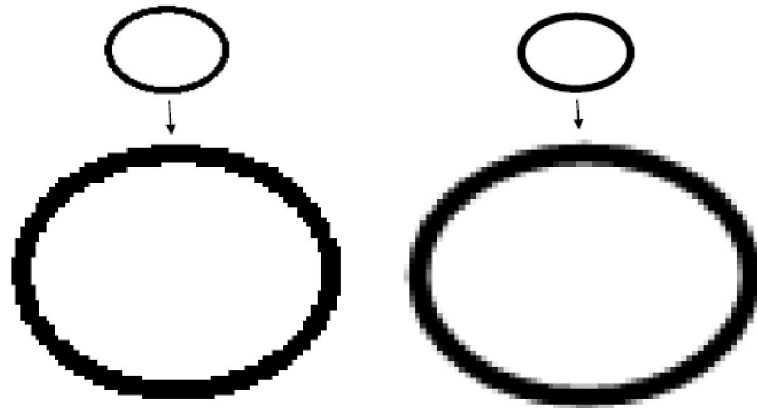




Problems with Aligned Ellipses

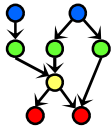


- ▶ Now in ENE octant, not ESE octant
- ▶ This problem is an artifact of *aliasing*, remember filter?



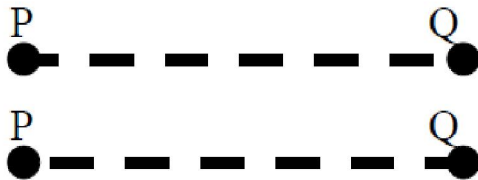
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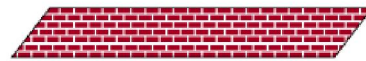
Patterned Lines

- ▶ Patterned line from P to Q is not same as patterned line from Q to P .



- ▶ Patterns can be *cosmetic* or *geometric*
 - ▶ Cosmetic: Texture applied after transformations
 - ▶ Geometric: Pattern subject to transformations

Cosmetic patterned line

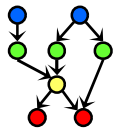


Geometric patterned line

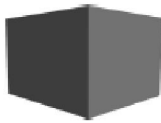


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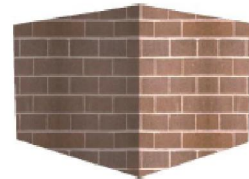
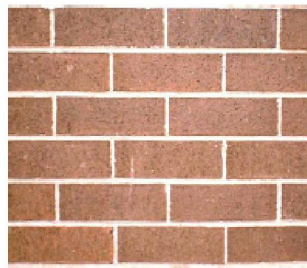




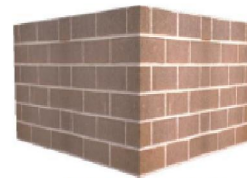
Geometric vs. Cosmetic



+



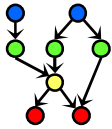
Cosmetic (Real-World
Contact Paper)



Geometric
(Perspectivized/Filtered)

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Non-Integer Primitives & General Conics

- ▶ **Non-Integer Primitives**
 - ▶ Initialization is harder
 - ▶ Endpoints are hard, too
 - ▶ making Line (P, Q) and Line (Q, R) join properly is a good test
 - ▶ Symmetry is lost
- ▶ **General Conics**
 - ▶ Very hard--the octant-changing test is tougher, the difference computations are tougher, etc.
 - ▶ Do it only if you have to
 - ▶ Note that drawing gray-scale conics is easier than drawing B/W conics

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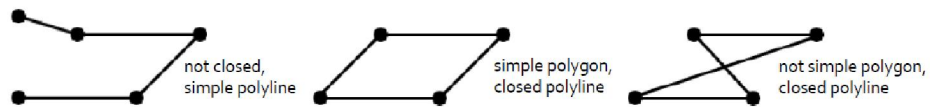




2-D Object Definition [1]

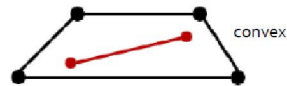
▶ Lines and polylines:

- ▶ Polylines: lines drawn between ordered points
- ▶ A closed polyline is a polygon, a simple polygon has no self-intersections



▶ Convex and concave polygons:

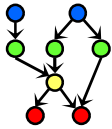
- ▶ Convex: For every pair of points inside the polygon, the line between them is entirely inside the polygon.
- ▶ Concave: For some pair of points inside the polygon, the line between them is not entirely inside the polygon. Not Convex.



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 Shapes
 Slide 2 (fall, 2010)
<http://bit.ly/h2VZn8>

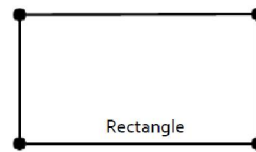
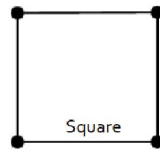
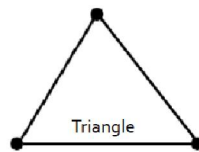
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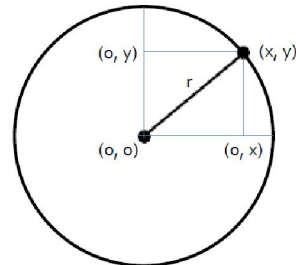
2-D Object Definition [2]

▶ Special Polygons:

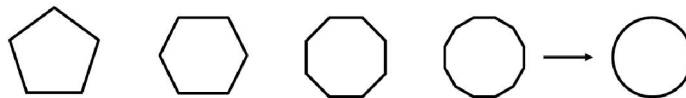


▶ Circles:

- ▶ Set of all points equidistant from one point called the center
- ▶ The distance from the center is the radius r
- ▶ The equation for a circle centered at (o, o) is $r^2 = x^2 + y^2$



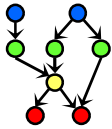
- ▶ A circle can be approximated by a polygon with many sides.



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Shapes
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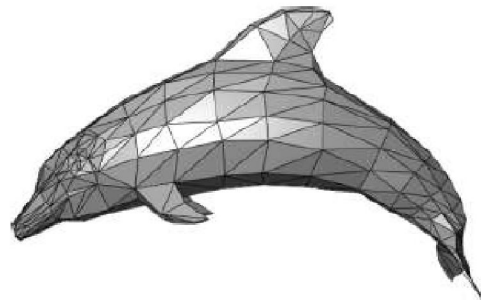




Triangle Meshes

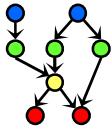
- ▶ Most common representation of shape in three dimensions
 - ▶ All vertices of triangle are guaranteed to lie in one plane (not true for quadrilaterals or other polygons)
 - ▶ Uniformity makes it easy to perform mesh operations such as subdivision, simplification, transformation etc.
 - ▶ Many different ways to represent triangular meshes
-
- ▶ See chapters 9 and 28 in book, en.wikipedia.org/wiki/polygon_mesh
 - ▶ Mesh transformation and deformation
 - ▶ Procedural generation techniques (upcoming labs on simulating terrain)

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 Shapes
 Slide 13 (fall, 2010)
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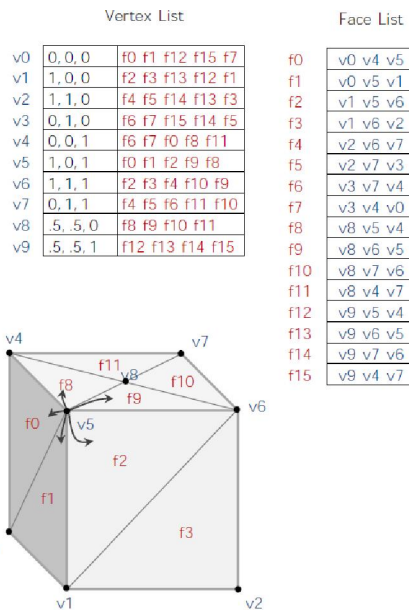
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Triangular Mesh Representation

- ▶ Vertex and face tables, analogous to 2D vertex and edge tables
- ▶ Each vertex listed once, triangles listed as ordered triplets of indices into the vertex table
 - ▶ Edges inferred from triangles
 - ▶ It's often useful to store associated faces with vertices (i.e. computing normals: vertex normal average of surrounding face normals)
- ▶ Vertices listed in counter clockwise order in face table.
 - ▶ No longer just because of convention. CCW order differentiates front and back of face

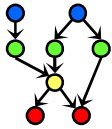


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Shapes
Slide 14 (fall, 2010)
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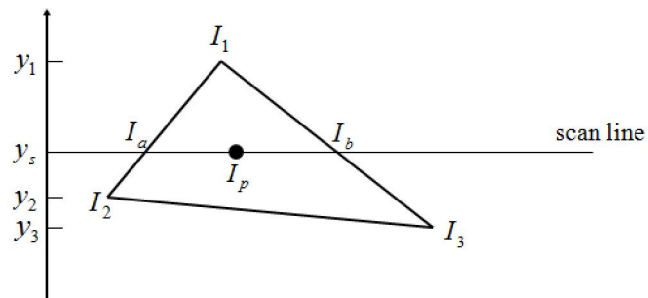
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General Polygons [1]: Scan Line Interpolation

- 1. Interpolate Value Along Polygon Edges to Get I_a, I_b
- 2. Interpolate Value Along Scan Lines to Get I_p



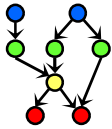
$$I_a = I_1 \frac{y_s - y_2}{y_1 - y_2} + I_2 \frac{y_1 - y_s}{y_1 - y_2}$$

$$I_b = I_1 \frac{y_s - y_3}{y_1 - y_3} + I_3 \frac{y_1 - y_s}{y_1 - y_3}$$

$$I_p = I_a \frac{x_b - x_p}{x_b - x_a} + I_b \frac{x_p - x_a}{x_b - x_a}$$

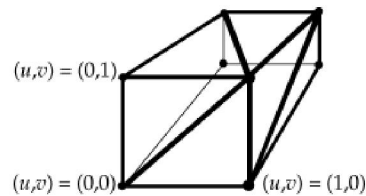
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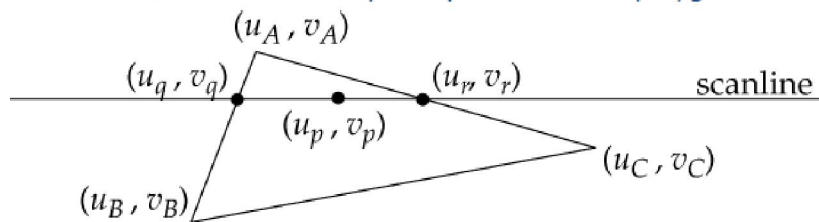


General Polygons [2]: Texture Mapping Preview

- ▶ Texture mapping polygons
 - ▶ (u, v) texture coordinates are pre-calculated and specified per vertex
 - ▶ Vertices may have different texture coordinates for different faces



- ▶ Texture coordinates are linearly interpolated across polygon



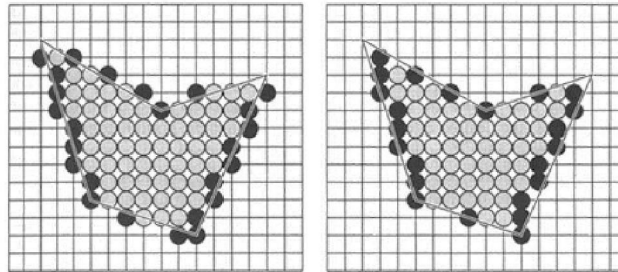
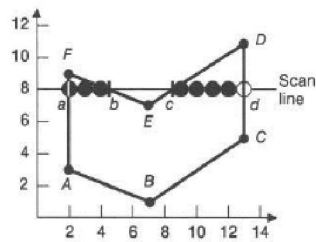
Brown University CS123
(Polygons &) Texture
Mapping
Slide 7 (fall, 2010)
<http://bit.ly/h2VZn8>

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General Polygons [3]: Continuity and Scan Line Interpolation

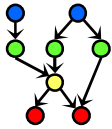


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Scan Conversion
Slide 43 (fall, 2010)
<http://bit.ly/hfbF0D>

- ▶ what's the difference between these two solutions? Under which circumstances is the right one "better"?

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Summary

- **Last Time: Clipping and Culling**
 - * What parts of scene to clip: edges vs. polygons of model
 - * What parts of viewport to clip against: clip faces vs. clip edges
 - * Cohen-Sutherland clipping: outcodes, simultaneous equations
 - * Liang-Barsky / Cyrus-Beck clipping: parametric equations
 - * Visibility culling: view frustum, back face, occlusion
- **Today: Scan Conversion, Concluded**
 - * Circles and ellipses
 - * Polygons: scan line interpolation (for flat/constant shading)
 - * Later: Gouraud & Phong shading, z-buffering, texture mapping
- **Excerpts from Van Dam notes, Brown CS123**
 - * Scan converting circles/ellipses
 - * Polygons
 - * Triangle meshes
 - * Scan line interpolation





Terminology

- **Scan Conversion (aka Rasterization)**
 - * **Given:** geometric object (e.g., circle, ellipse, projected polygon)
 - * **Decide:** what pixels to light (turn on; later, color/shade)
 - * **Basis:** what part of pixels crossed by object
- **Issues (Reasons why Scan Conversion is Nontrivial Problem)**
 - * **Aliasing** (e.g., **jaggies**) – discontinuities in lines
 - * **Cracks:** discontinuities in “polygon” mesh
- **Drawing Circles & Ellipses**
 - * **Incremental algorithm** – uses rounding, floating point arithmetic
 - * **Forward differences** – precalculated amounts to add to running total
 - * **Decision variable** – value whose sign indicates which pixel is next
- **Drawing Polygons**
 - * **Texture mapping** – finding pixels of image (texture) to put in polygon
 - * **Scan line interpolation** – procedure for filling in closed curves

