


## Lecture 10

# Curves and Surfaces Concluded 3-D Graphics Data Structures

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William H. Hsu  
Department of Computing and Information Sciences, KSU  
<http://www.cis.ksu.edu/~bhsu>


Readings:  
Sections 11.3, 12.1-12.5, Foley *et al*  
(Reference) [9](#), [10.1](#), 10.6-10.13, 10.16-10.17 Hearn and Baker 2<sup>o</sup>  
Slide Set 5, VanDam (8b, 11/09/1999)



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## Lecture Outline


- Readings
  - Sections 11.3, 12.1-12.5, Foley *et al*
  - Optional reference: Chapter [9](#), [10.1](#), 10.6-10.13, 10.16-10.17, Hearn and Baker 2<sup>o</sup>
- Quick Review: Properties of Cubic Curves and Splines
  - Splines:  $B$ - (UN, NUN, NUR = NURBS), Beta- ( $\beta$ -), Catmull-Rom, Kochanek-Bartels
  - Uniformity, rationality, continuity, control point and polygon properties
- Interpolating Cubic Curves and Surfaces
  - deCasteljau's algorithm for curves
  - Bicubic surface interpolation (concluded)
- 3D Graphics Data Structures
  - This time: boundary representations (aka B-reps)
  - Next time: spatial partitioning representations
- Visible Surface Determination (VSD): Introduction
  - Role of graphics data structures in VSD (more later)
  - Graphics data structures in computational geometry
- Next Lecture: Basics of Constructive Solid Geometry (Survey)



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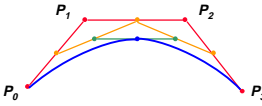
## Comparison of Cubic Curves

- Hermite
  - Blend 4 functions; no CP; full interpolation;  $C^1$  and  $G^1$  with constraints; fast
- Bézier
  - Convex CP; interpolate 2 of 4 control points;  $C^1$  and  $G^1$  with constraints; fastest
- B-splines
  - Uniform, nonrational
    - Convex CP, 4 points each, no interpolation;  $C^2$  and  $G^2$ ; medium
  - Nonuniform, nonrational
    - Convex CP, 5 points each, "no interpolation"; "up to"  $C^2$  and  $G^2$ ; slow
  - Nonuniform, rational
    - Convex CP, 5 points each, "no interpolation"; rational; "up to"  $C^2$  and  $G^2$ ; slow
- Beta Splines ( $\beta$ -Splines)
  - Convex CP; 6 points to control curve (4 local points, 2 global);  $C^1$  and  $G^2$ ; medium
- Catmull-Rom Splines
  - General CP; interpolate or approximate 4 points per CP;  $C^1$  and  $G^1$ ; medium
- Kochanek-Bartels Splines
  - General CP; interpolate 7 points per CP;  $C^1$  and  $G^1$ ; medium




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## Interpolating Curves [1]: Recursive Subdivision



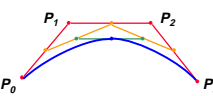
- Intuitive Idea
  - Given
    - Curve (Bézier or uniform B-spline) defined using control polygons (CPs)
    - 4 control points  $P_0, P_1, P_2, P_3$
  - Problem: can't get quite the right curve shape (not enough control points)
  - Solutions: increase degree of polynomial segments OR add CPs
  - Technique: recursive subdivision algorithm
    - Add control points by splitting existing CP up recursively
    - Compute CPs for left curve  $L_0, L_1, L_2, L_3$ , right curve  $R_0, R_1, R_2, R_3$
    - Stop when variation (curve-to-control point distance) is low enough
    - Purpose: display curve OR allow new control points to be manipulated




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## Interpolating Curves [2]: deCasteljau's Algorithm


- Recursive Subdivision Algorithm for Interpolation [deCasteljau, 1959]
  - Purpose: display curve OR allow new control points to be manipulated
  - Display: fast and cheap (see below)
- Properties
  - Cheap: can implement using subdivision matrices (Equations 11.52, 11.53, FVD)
  - Fast: rapid convergence due to...
  - Variation-diminishing property
    - Monotonic convergence to curve
    - Holds for all splines with convex-hull CPs
- When Does It Work?
  - Uniform splines (uniformly-spaced knots)
    - Q: Can we subdivide NURBS?
    - A: Yes, by adding knots (expensive) [Böhm, 1980; Cohen *et al*, 1980]
  - Alternative approach: hierarchical B-splines [Forsey and Bartels, 1988]






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## Quick Review: Bicubic Surfaces



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## Quick Review: Interpolating Bicubic Surfaces

  
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## Paper Reviews [1]: General Information


- **3 of 4 (Assigned) Reviews Required**
  - All reviews worth 15% of course grade
  - Choose 3 of 4 (*may have > 1 choice on some*) or write all 4
  - Lowest dropped (each of remaining 3 worth 50 of 1000 points)
- **General Objectives**
  - Compare, evaluate CG techniques (synthesis, processing, visualization)
  - Guidelines: next ([suggested topics](#), tools to appear on CIS 736 course web page)
- **Review Topics**
  - [Modeling](#), [rendering](#), [animation](#), [information visualization](#)
  - Selection criteria: target length 10 pages; no more than 15 pages
- **Logistics**
  - **Papers will be available online (and at 17 Seaton Hall) next week**
  - Send to CIS 736 GTA (Songwei Zhou) at [cis736ta@ringil.cis.ksu.edu](mailto:cis736ta@ringil.cis.ksu.edu)
  - Turn in by midnight of due date (no late reviews)
  - Get back commented reviews in electronic form

  
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## Paper Reviews [2]: Specific Objectives


- **Modeling**
  - "The right *representation* is half the battle"
  - "Graphics database formats + rendering / animation algorithms = CG programs"
- **Rendering**
  - Image synthesis: aspects of realism
  - "The right tool for the right job"
- **Animation**
  - What's beneficial, what's overkill?
  - What's easy, what's hard?
- **Information Visualization**
  - How to avoid "saying nothing" and "telling lies" with graphs
  - How to maximize information, not "ink" (screen / disk usage, etc.)
- **Overall: Be Able To**
  - Justify using CG technique *X* in scenario *S*
  - Select and develop appropriate (practical) CG techniques

  
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## Paper Reviews [3]: Do's and Don'ts


- **Do**
  - Use typical
    - Font (Times, Arial, etc.), type size (10-12 point), spacing (single), margins
    - Length (1-2 pages)
  - [Cite your sources](#)
  - Use spelling and grammar checkers (and check carefully by hand)
  - Write in [complete sentences](#) and your own words
  - [Discuss](#) paper
    - Significance, audience
    - Pros, cons (*Does CG method meet objectives? Why or why not?*)
    - Applications *you* would like to see in future work
    - Open (unanswered) questions! (Read carefully...)
- **Don't**
  - Merely
    - Quote paper, authors, bibliographic references, or other reviews
    - Summarize content of paper without evaluation and discussion
  - Critique without justification ("*This paper was (bad | vague | great.)*")

  
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## Terminology


- **Interpolation versus Approximation (Section 10.6, Hearn and Baker)**
  - [Interpolation](#): fit curve *through* specified points
  - [Approximation](#): fit curve to control path (without necessarily passing through)
- **deCasteljau's Algorithm: Recursive Subdivision Algorithm for Interpolation**
- **Bicubic Surfaces**
  - Types: [Hermite](#) (11.3.1 FVD), [Bézier](#) (11.3.2 FVD), [B-splines](#) (11.3.3 FVD)
  - [Coons patch](#): generalization of Hermite patch form to arbitrary [boundary curves](#)
- **3D Graphics Data Structures**
  - [Regularized Boolean set operations](#):  $\cup$ ,  $\cap$ ,  $-$  (12.2 FVD)
  - [Primitive instancing](#): parameterized object-like 3D solid representation (12.3 FVD)
  - [Sweep representations](#): objects moved along trajectory define others (12.4 FVD)
  - [Boundary representations aka B-reps](#): vertex, edge, face descriptions (12.5 FVD)
    - [Polyhedra](#): solid bounded by polygons, satisfying [Euler's formula](#) (12.5.1 FVD)
    - [Winged edge](#): vertex-edge-face data structure (12.5.2 FVD)
    - [Composition](#) of B-reps using Boolean set operations (12.5.3 FVD)

  
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## Summary Points

- **Quick Review: Properties of Cubic Curves and Splines**
- **Interpolating Cubic Curves and Surfaces**
  - deCasteljau's algorithm for curves – 11.2.7 FVD
  - Bicubic surface interpolation (concluded) – 11.3.5 FVD
- **3D Graphics Data Structures (Chapter 12, FVD)**
  - Representing solids – 12.1 FVD
  - Regularized Boolean set operations, primitive instancing, sweep representations
  - Boundary representations (*aka B-reps*) – 12.5 FVD
    - Polyhedra, winged edge (Mantyla)
    - Composition of B-reps using Boolean set operations
- **Role of Graphics Data Structures in Visible Surface Determination (VSD)**
- **Next Lecture**
  - [Spatial partitioning representations](#) – 12.6 FVD
    - Cell decomposition
    - Quadrees and octrees
  - Basics of [Constructive Solid Geometry \(CSG\)](#)

  
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