





























































Summary

- Cumulative Transformation Matrices (CTM): T, R, S
 - * Translation
 - * Rotation
 - * Scaling
 - * Setup for Shear/Skew, Perspective to Parallel see Eberly, Foley et al.
- "Matrix Stack" in OpenGL: Premultiplication of Matrices
- Coming Up
 - * Parametric equations in clipping
 - * Intersection testing: ray-cube, ray-sphere, implicit equations (ray tracing)
- Homogeneous Coordinates: What Is That 4th Coordinate?
 - * http://en.wikipedia.org/wiki/Homogeneous_coordinates
 - * Crucial for ease of normalizing T, R, S transformations in graphics
 - * See: Slide 14 of this lecture
 - * Note: Slides 20 & 23 (T, S) versus 21 (R)
 - * Read about them in Eberly 2e, Angel 3e
 - * Special case: barycentric coordinates





Terminology

- <u>Cumulative Transformation Matrices (CTM): Translation, Rotation, Scaling</u>
- Some Basic Analytic Geometry and Linear Algebra for CG
 - * Vector space (VS) set of vectors: addition, scalar multiplication; VS axioms
 - * Affine space (AS) set of points with associated VS: vector difference, point-vector addition; AS axioms
 - * Linear subspace nonempty subset S of VS (V, +, ·) closed under + and ·
 - * Affine subspace nonempty subset S of VS (V, +, ·) such that closure S' of S under point subtraction is a linear subspace of V
 - * <u>Dot product</u> scalar-valued <u>inner product</u> $\langle u, v \rangle \equiv u \cdot v \equiv u_1 v_1 + u_2 v_2 + ... + u_n v_n$
 - * Orthogonality property of vectors \mathbf{u} , \mathbf{v} that $\mathbf{u} \cdot \mathbf{v} = \mathbf{0}$
 - * Orthonormality basis containing pairwise-orthogonal unit vectors
 - * Length (Euclidean norm) $\|v\| = \sqrt{v \cdot v}$
 - * Rigid body transformation one that preserves distance between points
 - * Homogeneous coordinates (esp. barycentric coordinates) allow affine, projective transformations; "4-D" space for 3-D CG

636 & 736

ion to) Computer Graphics

Lect

Lecture 1 of 41

outing & Information Science

puting & Information Scienc Kansas State Universi