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Scan Conversion 1 of 2: Midpoint Algorithm for Lines and Ellipses

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KSOL course pages: <u>http://bit.ly/hGvXIH</u> / <u>http://bit.ly/eVizrE</u> Public mirror web site: <u>http://www.kddresearch.org/Courses/CIS636</u> Instructor home page: <u>http://www.cis.ksu.edu/~bhsu</u>

Readings:

Today: Sections 2.5.1, 3.1, Eberly 2^e – see <u>http://bit.ly/ieUq45</u> This week: Brown CS123 slides on Scan Conversion – <u>http://bit.ly/hfbF0D</u> Wayback Machine archive of Brown CS123 slides: <u>http://bit.ly/gAhJbh</u>

CIS 536/636 Introduction to Computer Graphics

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3			Where We A	re
		Lecture	Topic	Primary Source(s)
		0	Course Overview	Chapter 1, Eberly 2 ^e
		1	CG Basics: Transformation Matrices; Lab 0	Sections (§) 2.1, 2.2
		2	Viewing 1: Overview, Projections	§ 2.2.3 – 2.2.4, 2.8
		3	Viewing 2: Viewing Transformation	§ 2.3 esp. 2.3.4; FVFH slides
		4	Lab 1a: Flash & OpenGL Basics	Ch. 2, 16 ¹ , Angel Primer
		5	Viewing 3: Graphics Pipeline	§ 2.3 esp. 2.37:26.27
		6	Scan Conversion 1: Lines, Midpoint Algorithm	§ 2.5.1, 3.1; FVFH slides
		7	Viewing 4: Clipping & Culling; Lab 1b	§ 2.3.5, 2.4, 3.1.3
		8	Scan Conversion 2: Polygons, Clipping Intro	§ 2.4, 2.5 esp. 2.5.4, 3.1.6
		9	Surface Detail 1: Illumination & Shading	§ 2.5, 2.6.1 – 2.6.2, 4.3.2, 20.2
		10	Lab 2a: Direct3D / DirectX Intro	§ 2.7, Direct3D handout
		11	Surface Detail 2: Textures; OpenGL Shading	§ 2.6.3, 20.3 – 20.4, Primer
		12	Surface Detail 3: Mappings; OpenGL Textures	§ 20.5 – 20.13
		13	Surface Detail 4: Pixel/Vertex Shad.; Lab 2b	§ 3.1
		14	Surface Detail 5: Direct3D Shading; OGLSL	§ 3.2 – 3.4, Direct3D handout
		15	Demos 1: CGA, Fun; Scene Graphs: State	§ 4.1 – 4.3, CGA handout
		16	Lab 3a: Shading & Transparency	§ 2.6, 20.1, Primer
		17	Animation 1: Basics, Keyframes; HW/Exam	§ 5.1 – 5.2
			Exam 1 review; Hour Exam 1 (evening)	Chapters 1 – 4, 20
		18	Scene Graphs: Rendering; Lab 3b: Shader	§ 4.4 – 4.7
		19	Demos 2: SFX; Skinning, Morphing	§ 5.3 – 5.5, CGA handout
		20	Demos 3: Surfaces; B-reps/Volume Graphics	§ 10.4, 12.7, Mesh handout
		Lightly-sh machine p shaded er Green, bl	aded entries denote the due date of a written problem set; problem (programming assignment); blue-shaded entries, t ntry, that of the term project. lue and red letters denote exam review, exam, and exam	heavily-shaded entries, that of a hat of a paper review; and the green-
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4	Review:					
	CTM for "Polygons-to-Pixels" Pipeline					
	 Entire problem can be reduced to a composite matrix multiplication of vertices, clipping, and a final matrix multiplication to produce screen coordinates. 					
	 Final composite matrix (CTM) is composite of all modeling (instance) transformations (CMTM) accumulated during scene graph traversal from root to leaf, composited with the final composite normalizing transformation N applied to the root/world coordinate system: 					
	1) $N = D_{persp} S_{far} S_{xy} M_{rot} T_{trans}$					
	2) $CTM = N \cdot CMTM$					
	3) $P' = CTM \cdot P$ for every vertex P defined in its own coordinate system					
	4) $P_{screen} = 512 \cdot P' + 1$ for all clipped P'					
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Basic Algorithm

- Find equation of line that connects two points P and Q
- Starting with leftmost point, increment x_i by 1 to calculate y_i = m * x_i + B where m = slope, B = y intercept
- Draw pixel at (x_i, Round(y_i)) where Round (y_i) = Floor (0.5 + y_i)

Incremental Algorithm:

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- > Each iteration requires a floating-point multiplication
 - > Modify algorithm to use deltas
 - $(y_{i+1} y_i) = m * (x_{i+1} x_i) + B$
 - ▶ $y_{i+1} = y_i + m * (x_{i+1} x_i)$
 - If $\Delta x = 1$, then $y_{i+1} = y_i + m$
- At each step, we make incremental calculations based on preceding step to find next y value

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Strategy 2: Midpoint Line Algorithm [3]

- Line passes between E and NE
- Point that is closer to intersection point Q must be chosen
- Observe on which side of line midpoint *M* lies:
 - E is closer to line if midpoint *M* lies above line, i.e., line crosses bottom half
 - NE is closer to line if midpoint *M* lies below line, i.e., line crosses top half
- ▶ Error (vertical distance between chosen pixel and actual line) is always $\leq .5$

























