

## Lecture 31 of 41

# Ray Tracing, Part 1 of 2: Intersections, Ray Trees & Recursion

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KSOL course pages: <http://bit.ly/hGvXIH> / <http://bit.ly/eVizrE>

Public mirror web site: <http://www.kddresearch.org/Courses/CIS636>

Instructor home page: <http://www.cis.ksu.edu/~bhsu>

### Readings:

Last class: §5.3, Eberly 2<sup>e</sup> – see <http://bit.ly/ieUq45>; CGA Handout

Today: Chapter 14, Eberly 2<sup>e</sup>

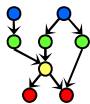
Next class: Ray Tracing Handout

Reference – Wikipedia, Ray Tracing: <http://bit.ly/dV7INm>

Reference – ACM Ray Tracing News: <http://bit.ly/fqyZNQ>



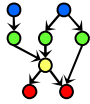
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## Lecture Outline

- Reading for Last Class: §5.3, Eberly 2<sup>e</sup>; CGA Handout
- Reading for Today: Chapter 14, Eberly 2<sup>e</sup>
- Reading for Next Class: Ray Tracing Handout
- Last Time: Animation Part 3 of 3 – Inverse Kinematics
  - \* FK vs. IK
  - \* IK
    - Autonomous agents vs. hand-animated movement
    - Analytical vs. iterative solutions
  - \* Rag doll physics, rigid-body dynamics, physically-based models
- End of Material on: Particle Systems, Collisions, CGA, PBM
- Today: Ray Tracing, Part 1 of 2
  - \* Vectors: Light/shadow (L), Reflected (R), Transmitted/refracted (T)
  - \* Basic recursive ray tracing: ray trees
- Next Class: Ray Tracing Lab



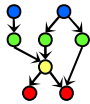


## Where We Are

21	Lab 4a: Animation Basics	Flash animation handout
22	Animation 2: Rotations; Dynamics, Kinematics	Chapter 17, esp. §17.1 – 17.2
23	Demos 4: Modeling & Simulation; Rotations	Chapter 10 <sup>1</sup> , 13 <sup>2</sup> , §17.3 – 17.5
24	Collisions 1: axes, OBBs, Lab 4b	§2.4.3, 8.1, GL handout
25	Spatial Sorting: Binary Space Partitioning	Chapter 6, esp. §6.1
26	Demos 5: More CGA; Picking; HW/Exam	Chapter 7 <sup>4</sup> ; § 8.4
27	Lab 5a: Interaction Handling	§ 8.3 – 8.4; 4.2, 5.0, 5.6, 9.1
28	Collisions 2: Dynamic, Particle Systems	§ 9.1, particle system handout
	Exam 2 review; Hour Exam 2 (evening)	Chapters 5 – 6, 7 <sup>4</sup> – 8, 12, 17
29	Lab 5b: Particle Systems	Particle system handout
30	Animation 3: Control & IK	§ 5.3, CGA handout
31	Ray Tracing 1: Intersections, Ray Trees	Chapter 14
32	Lab 6a: Ray Tracing Basics with POV-Ray	RT handout
33	Ray Tracing 2: advanced topic survey	Chapter 15, RT handout
34	Visualization 1: Data (Quantities & Evidence)	Tufte handout (1)
35	Lab 6b: More Ray Tracing	RT handout
36	Visualization 2: Objects	Tufte handout (2 & 4)
37	Color Basics; Term Project Prep	Color handout
38	Lab 7: Fractals & Terrain Generation	Fractals/Terrain handout
39	Visualization 3: Processes; Final Review 1	Tufte handout (3)
40	Project presentations 1; Final Review 2	–
41	Project presentations 2	–
	Final Exam	Ch. 1 – 8, 10 – 15, 17, 20

Lightly-shaded entries denote the due date of a written problem set; heavily-shaded entries, that of a machine problem (programming assignment); blue-shaded entries, that of a paper review; and the green-shaded entry, that of the term project.

Green, blue and red letters denote exam review, exam, and exam solution review dates.



## Acknowledgements: Inverse Kinematics, Ray Tracing



### David C. Brogan

Visiting Assistant Professor, Computer Science Department, University of Virginia

<http://www.cs.virginia.edu/~dbrogan/>

Susquehanna International Group (SIG)

<http://www.sig.com>



Computer Science  
at the UNIVERSITY of VIRGINIA



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Ph.D. Candidate

Mechanical Engineering Department

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### Dave Shreiner & Brad Grantham

Adjunct Professor & Adjunct Lecturer,

Santa Clara University

ARM Holdings, plc

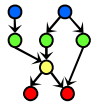
<http://www.plunk.org/~shreiner/>

<http://www.plunk.org/~grantham/>



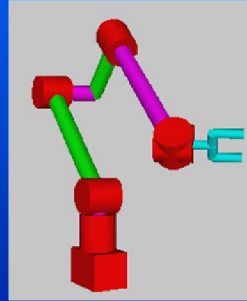
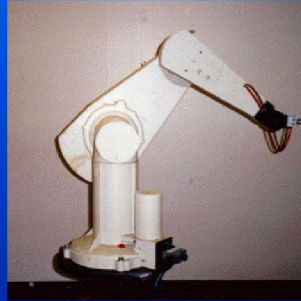
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## Review [1]: Kinematics & Degrees of Freedom

- How about this robot arm?

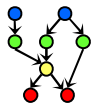


- Six again
  - 2-base, 1-shoulder, 1-elbow, 2-wrist

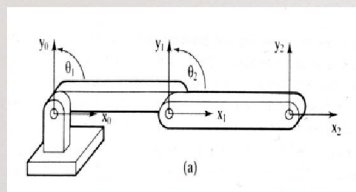
Adapted from slides ♥ 2000 – 2005 D. Brogan, University of Virginia  
CS 551, Advanced CG & Animation – <http://bit.ly/hUXrqd>



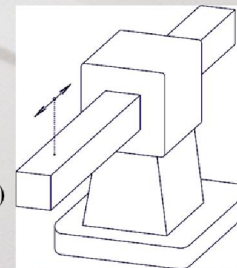
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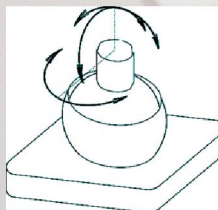
## Review [2]: Joint Types



Revolute Joint  
1 DOF ( Variable -  $\theta$  )



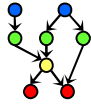
Prismatic Joint  
1 DOF (linear) (Variables -  $d$  )



Spherical Joint  
3 DOF ( Variables -  $\theta_1, \theta_2, \theta_3$  )

Adapted from slides ♥ 2002 R. Melamud, Stanford University  
Mirrored at CMU 16-311 Introduction to Robotics, <http://generalrobotics.org>





## Forward Kinematics: Joint Angles to Bone Coordinates

- We will use the vector:

$$\Phi = [\phi_1 \quad \phi_2 \quad \dots \quad \phi_M]$$

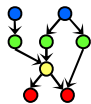
to represent the array of M joint DOF values

- We will also use the vector:

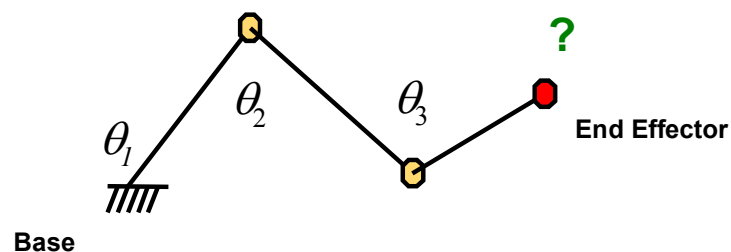
$$\mathbf{e} = [e_1 \quad e_2 \quad \dots \quad e_N]$$

to represent an array of N DOFs that describe the end effector in world space. For example, if our end effector is a full joint with orientation,  $\mathbf{e}$  would contain 6 DOFs: 3 translations and 3 rotations. If we were only concerned with the end effector position,  $\mathbf{e}$  would just contain the 3 translations.

Adapted from slides ♥ 2004 – 2005 S. Rotenberg, UCSD  
CSE169: Computer Animation, Winter 2005 – <http://bit.ly/f0ViAN>



## Review [3]: Forward Kinematics



$$\vec{\mathbf{x}} = f(\vec{\boldsymbol{\theta}})$$

Choi


$$\mathbf{e} = f(\Phi)$$

Rotenberg

Adapted from slides ♥ 2002 K. J. Choi, Seoul National University  
Graphics and Media Lab (<http://graphics.snu.ac.kr>) – mirrored at: <http://bit.ly/hnzSAN>

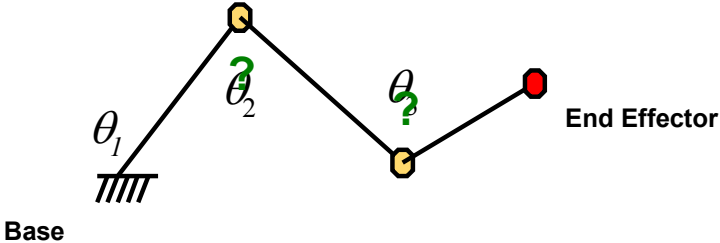


9



## Review [4]: Inverse Kinematics

For more on characters & IK, see:  
Advanced Topics in CG Lecture 05




$$\vec{\theta} = f^{-1}(\vec{x}) \quad \Phi = f^{-1}(\mathbf{e})$$

Choi                      Rotenberg

Adapted from slides ♥ 2002 K. J. Choi, Seoul National University  
Graphics and Media Lab (<http://graphics.snu.ac.kr>) – mirrored at: <http://bit.ly/hnzSAN>

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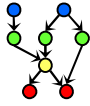
## Inverse Kinematics: Issues

- IK is challenging because while  $f()$  may be relatively easy to evaluate,  $f^{-1}()$  usually isn't
- For one thing, there may be several possible solutions for  $\Phi$ , or there may be no solutions
- Even if there is a solution, it may require complex and expensive computations to find it
- As a result, there are many different approaches to solving IK problems

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CSE169: Computer Animation, Winter 2005 – <http://bit.ly/f0ViAN>

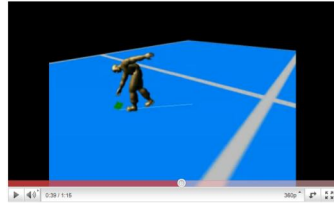
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11



## Review [5]: Inverse Kinematics Demos

Inverse Kinematics demo



© 2008 M. Kinzelman  
<http://youtu.be/l52yZ491kPo>

Inverse Kinematics Demonstration in Maya



© 2007 A. Brown  
<http://youtu.be/6JdLOLazJJ0>

Momentum-based Inverse Kinematics with Motion Capture



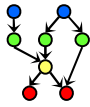
© 2008 T. Komura, H. S. Lim, & R. W. H. Lau  
<http://youtu.be/FJTBMnP6oCM>

PUMA robot playing golf



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<http://youtu.be/YvRBWIRAPsE>

12



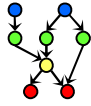
## Review [6]: Ragdoll Physics

- **Type of Procedural Animation**
  - \* Automatically generates CGA directives (rotations)
  - \* Based on simulation
  - \* Rigid-body dynamics
- **Articulated Figure**
  - \* Gravity
  - \* No autonomous movement
  - \* Used for inert body
    - Usually: character death (car impact, falling body, etc.)
    - Less often: unconscious, paralyzed character
- **Collisions with Multiple Bodies**
  - \* Inter-character
  - \* Character-object



Falling Bodies © 1997 – 2001 Animats  
<http://www.animats.com>





## Review [7]: Ragdoll Physics Demos

3ds max 8 Ragdoll Physics Test



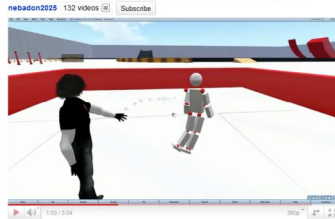
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<http://youtu.be/ohNqCb--aSs>

Ragdoll physics



© 2006 P. Pelt  
<http://youtu.be/6JdL0LazJJ0>  
See also: [http://youtu.be/5\\_Qisl0fyaU](http://youtu.be/5_Qisl0fyaU)

My Ninja Ragdoll (OpenSimulator Ninja/ODE Physics) OSGrid.org

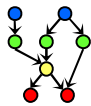


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[http://youtu.be/uW\\_DK2qvKv8](http://youtu.be/uW_DK2qvKv8)

Ragdoll Demo (Python + ODE)

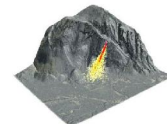


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<http://bit.ly/gUj9Su> / <http://youtu.be/FJTBmP6oCM>

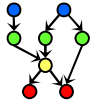


## Review [8]: Physically-Based Modeling (PBM)

- **Particle Dynamics**
  - \* **Emitters**
    - 0-D (points), 1-D (lines), 2-D (planes, discs, cross-sections)
    - e.g., fireworks (0-D); fountains (0/1/2-D); smokestacks, jets (2-D)
  - \* **Simulation:** birth-death process, functions of particle age/trajectory
- **Rigid-Body Dynamics**
  - \* **Constrained systems of connected parts**
  - \* **Examples:** falling rocks, colliding vehicles, rag dolls
- **Articulated Figures: Primarily IK**
- **More References**
  - \* **ACM, Intro to Physically-Based Modeling:** <http://bit.ly/hhQvXd>
  - \* **Wikipedia, Physics Engine:** <http://bit.ly/h4PIRt>
  - \* **Wikipedia, N-Body Problem:** <http://bit.ly/1ayWwe>
- **PBM System: nVidia (Ageia) PhysX:** <http://bit.ly/cp7bnA>

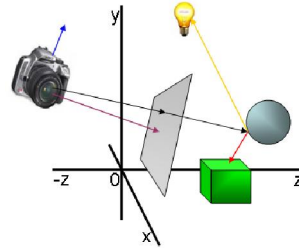


Rocks fall  
Everyone dies



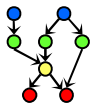
## Ray Tracing [1]: Overview

- What is it?
- Why use it?
- Basics
- Advanced topics
- References



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Cappemini Netherlands  
<http://bit.ly/erkKrC>

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## Ray Tracing [2]: Why Use It?

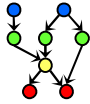
- Simulate rays of light
- Produces natural lighting effects
  - Reflection
  - Refraction
  - Soft Shadows
  - Depth of Field
  - Motion Blur
  - Caustics
- Hard to simulate effects with rasterization techniques (OpenGL)
- Rasterizers require many passes
- Ray-tracing easier to implement

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17



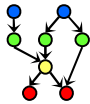
## Ray Tracing [3]: Who Uses It?

- Entertainment (Movies, Commercials)
- Games pre-production
- Simulation

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18



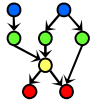
## Ray Tracing [4]: Brief History

- Decartes, 1637 A.D. - analysis of rainbow
- Arthur Appel, 1968 - used for lighting 3D models
- Turner Whitted, 1980 - “An Improved Illumination Model for Shaded Display” really kicked everyone off.
- 1980-now - Lots of research

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19



## Ray Tracing [5]: Basic Operations

- Generating Rays
- Intersecting Rays with Scene
- Lighting
- Shadowing
- Reflections

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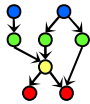
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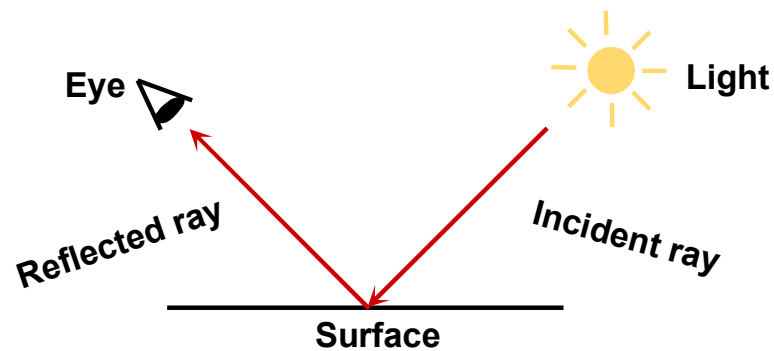
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## Ray Tracing [6]: Basic Idea

- Simulate light rays from light source to eye



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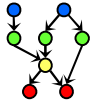
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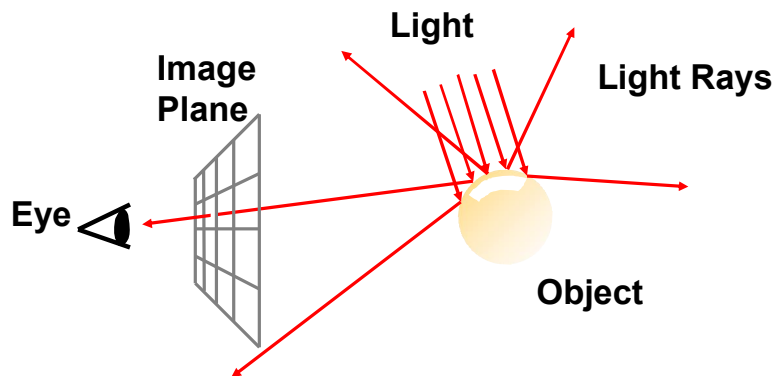
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## “Forward” Ray Tracing

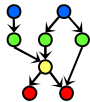
- Trace rays from light
- Lots of work for little return



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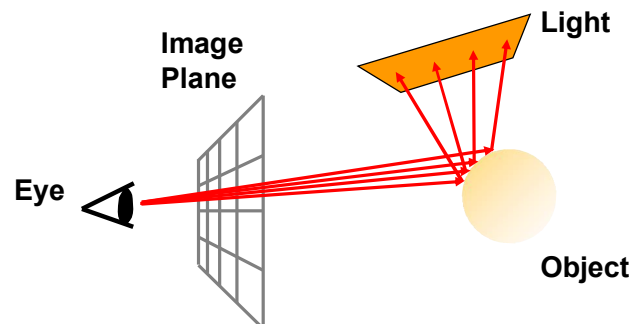


22



## “Backward” Ray Tracing

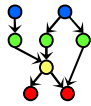
- Trace rays from eye instead
- Do work where it matters



*This is what most people mean by “ray tracing”.*

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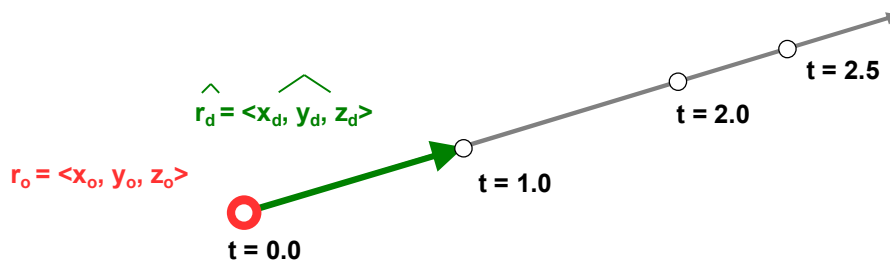


## Ray: Parametric Form

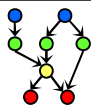
- Ray expressed as function of a single parameter ("t")

$$\langle x, y, z \rangle = \langle x_o, y_o, z_o \rangle + t * \langle x_d, y_d, z_d \rangle$$

$$\langle x, y, z \rangle = r_o + tr_d$$

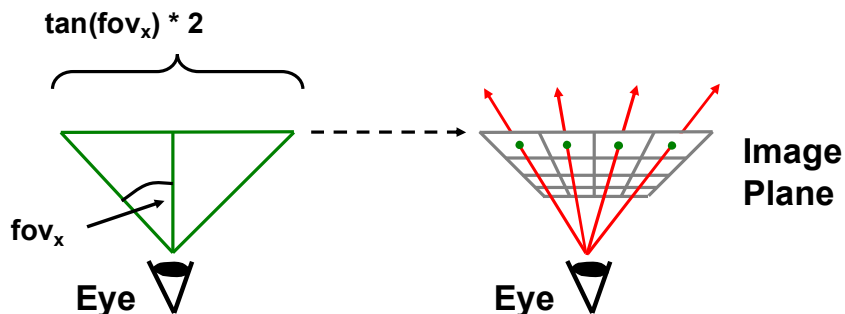


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## Generating Rays [1]

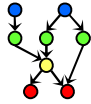
- Trace one ray for each pixel (u, v) in image plane



(Looking down from the top)

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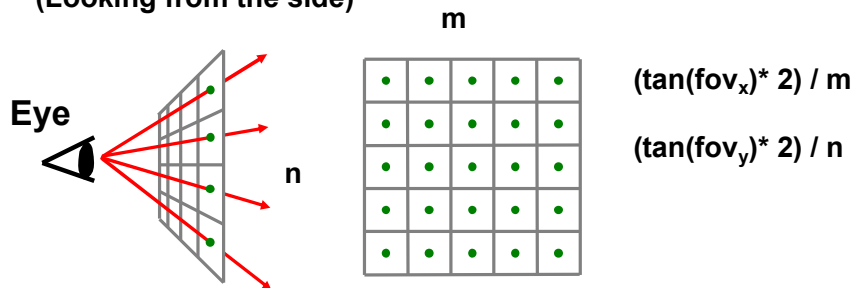




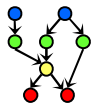
## Generating Rays [2]

- Trace one ray for each pixel  $(u, v)$  in image plane

(Looking from the side)



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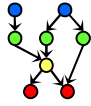
## Generating Rays [3]

- Trace one ray for each pixel  $(u, v)$  in image plane

```
renderImage() {
  for each pixel i, j in the image
    ray.setStart(0, 0, 0);    // r_o
    ray.setDir  ((.5 + i) * tan(fov_x) * 2 / m,
                (.5 + j) * tan(fov_y) * 2 / n,
                1.0);        // r_d
    ray.normalize();
    image[i][j] = rayTrace(ray);
}
```

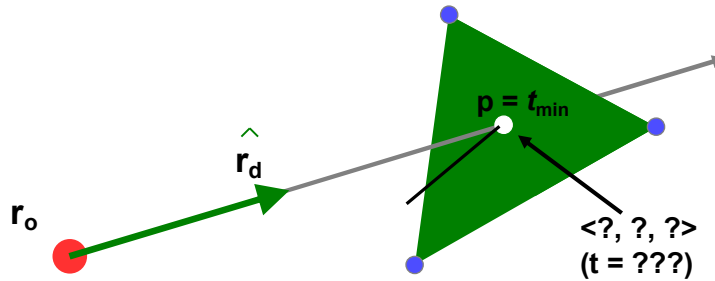
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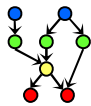


## Ray/Triangle Intersection [1]: Intersection Test Revisited

- Want to know: at what *point*  $p$  does ray intersect triangle?
- Compute lighting, reflected rays, shadowing *from that point*

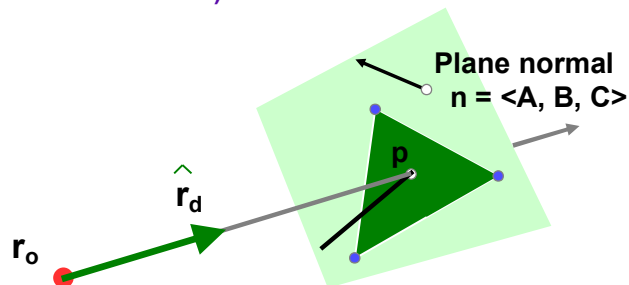


Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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## Ray/Triangle Intersection [2]: Ray/Plane Intersection Point $p$

- Step 1 : Intersect with plane  
(  $Ax + By + Cz + D = 0$  )

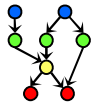


$$t_{\min} = p = -(n \cdot r_o + D) / (n \cdot r_d)$$

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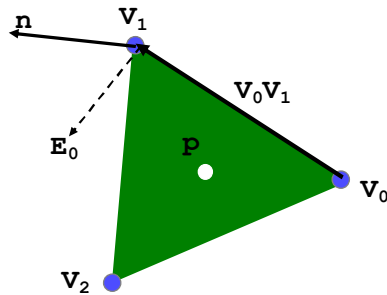






## Ray/Triangle Intersection [3]: Triangle Containment

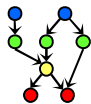
- Step 2 : Check against triangle edges



$$\begin{aligned} E_i &= V_i V_{i+1} \times n && (\text{plane A, B, C}) \\ d_i &= -A \cdot N && (\text{plane D}) \end{aligned}$$

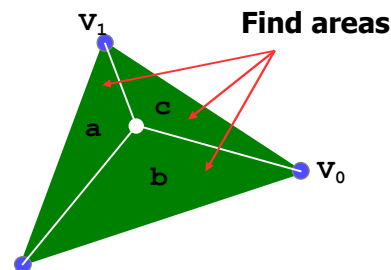
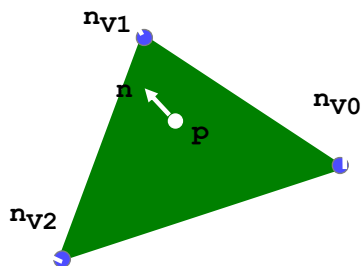
**Plug p into  $(p \cdot E_i + d_i)$  for each edge  
if signs are all positive or negative,  
point is inside triangle!**

Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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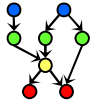
## Triangle Normals for Shading

- Could use plane normals (flat shading)
- Better to interpolate from vertices



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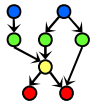


## Finding Intersections

- Check all triangles, keep closest intersection  $t_{\min}$

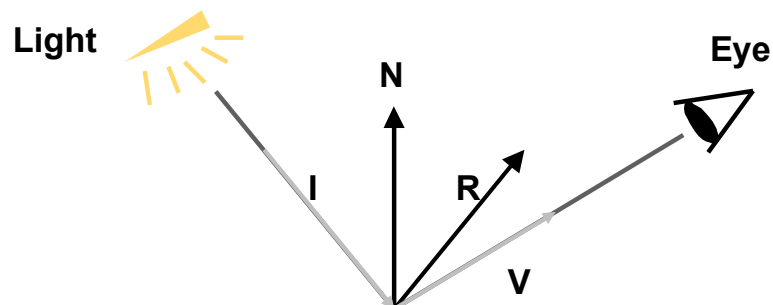
```
hitObject(ray) {
  for each triangle in scene
    does ray intersect triangle?
    if(intersected and was closer)
      save that intersection
  if(intersected)
    return intersection point and normal
}
```

Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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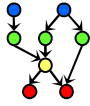
## Lighting [1]: General Notation Review

- We'll use triangles for lights
- Can build complex shapes from triangles
- Some lighting terms



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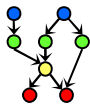
## Lighting [2]: Modified Phong Illumination

- Use modified Phong lighting
  - \* similar to OpenGL
  - \* simulates rough and shiny surfaces

for each light

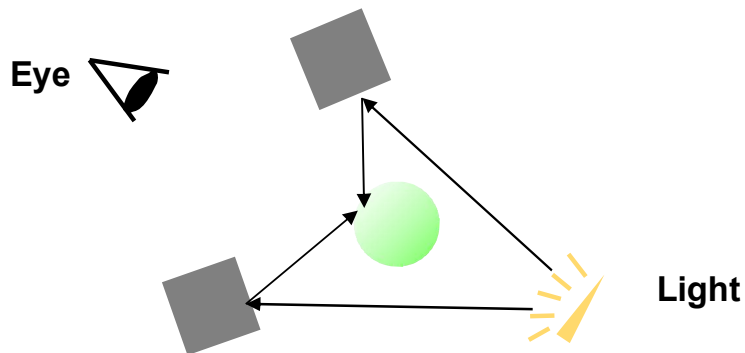
$$I_n = I_{\text{ambient}} K_{\text{ambient}} + I_{\text{diffuse}} K_{\text{diffuse}} (L \cdot N) + I_{\text{specular}} K_{\text{specular}} (R \cdot V)^n$$

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## Ambient Light

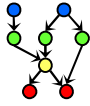
- $I_{\text{ambient}}$  – simulates indirect lighting in a scene



- May not need for RT!

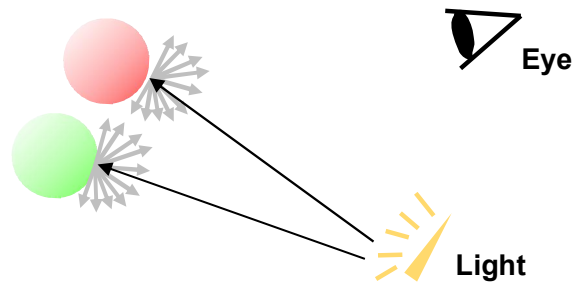
Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
COEN 290: Computer Graphics I, Winter 2001 – <http://bit.ly/hz1kfU>



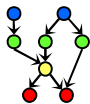


## Diffuse Light

- $I_{\text{diffuse}}$  – simulates direct lighting on rough surface
- Viewer-independent
- Paper, rough wood, brick, etc...

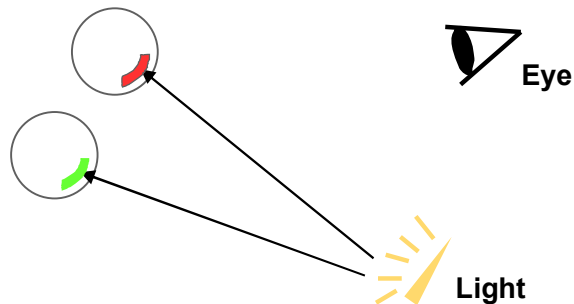


Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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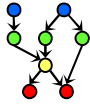
## Specular Light

- $I_{\text{specular}}$  simulates direct lighting on a smooth surface
- Viewer dependent
- Plastic, metal, polished wood, etc...



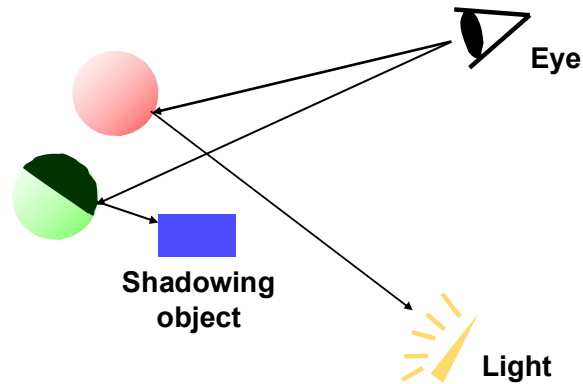
Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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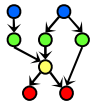


## Shadow Test

- Check against other objects to see if point is shadowed

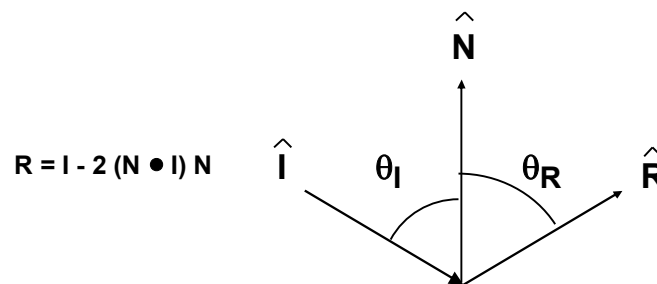


Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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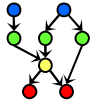
## Reflection

- Angle of incidence = angle of reflection ( $\theta_I = \theta_R$ )
- $I, R, N$  lie in the same plane



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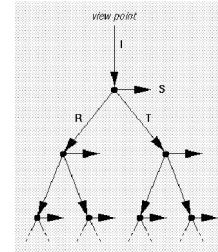




## Putting It All Together [1]: Recursive Calculation & Ray Tree

- Recursive ray evaluation

```
rayTrace(ray) {
    hitObject(ray, p, n, triangle);
    color = object color;
    if(object is light)
        return(color);
    else
        return(lightning(p, n, color));
}
```

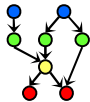


Ray tree  
© 2000 N. Patrikalakis, MIT  
<http://bit.ly/fjcGGk>

I = Incident ray  
S = light Source vector (aka L)  
R = reflected ray  
T = transmitted ray

- Generates ray tree shown at right

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## Putting It All Together [2]: Applying Lighting

- Calculating surface color

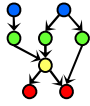
```
lighting(point) {
    color = ambient color;
    for each light
        if(hitObject(shadow ray))
            color += lightcolor *
                dot(shadow ray, n);
    color += rayTrace(reflection) *
        pow(dot(reflection, ray), shininess);
    return(color);
}
```

Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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41



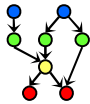
## Putting It All Together [3]: Main Program

```
main() {
    triangles = readTriangles();
    image = renderImage(triangles);
    writeImage(image);
}
```

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42

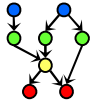


## Good Start: What next?

- Lighting, Shadows, Reflection are enough to make some compelling images
- Want better lighting and objects
- Need more speed

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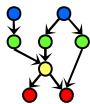




## More Quality, More Speed

- Better Lighting + Forward Tracing
- Texture Mapping
- Modeling Techniques
- Distributed Ray Tracing: Techniques
  - \* Motion Blur
  - \* Depth of Field
  - \* Blurry Reflection/Refraction
  - \* Wikipedia, *Distributed Ray Tracing*: <http://bit.ly/ihyVUs>
- Improving Image Quality
- Acceleration Techniques

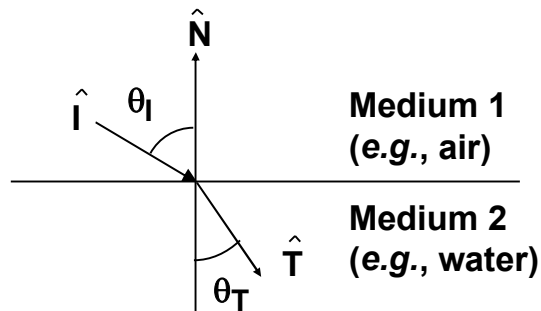
Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
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## Refraction [1]: Snell's Law

- Keep track of medium (air, glass, etc)
- Need *index of refraction* ( $\eta$ )
- Need solid objects

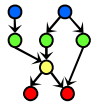
$$\frac{\sin(\theta_I)}{\sin(\theta_T)} = \frac{\eta_1}{\eta_2}$$



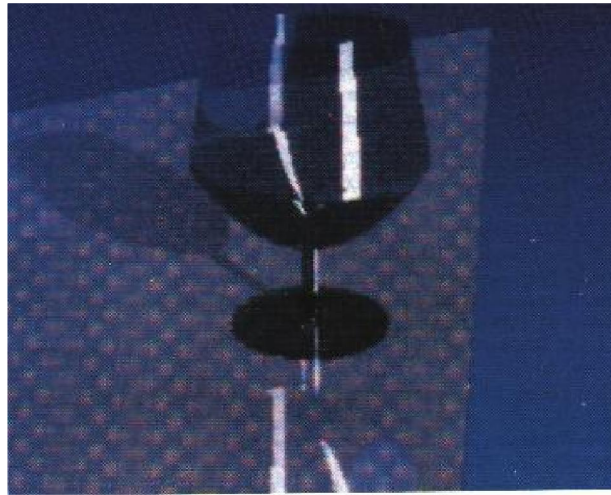
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45



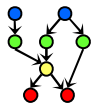
## Refraction [2]: Example



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46



## Improved Light Model: Cook-Torrance

- **Cook-Torrance model**
  - \* Based on a microfacet model
  - \* Wikipedia: <http://bit.ly/hX3U30>
- Metals have different color at angle
- Oblique reflections leak around corners

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- Backward tracing doesn't handle indirect lighting too well
- To get *caustics*, trace forward, store results in texture map

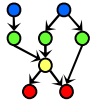


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## A 3D computer-generated scene featuring a blue glass sphere and a transparent blue cube resting on a red and white checkered floor. The sphere is on the left, casting a soft shadow. The cube is on the right, also casting a shadow and showing internal refractions. The background is a solid dark blue.



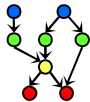
SANTA CLARA UNIVERSITY  
SCHOOL OF ENGINEERING



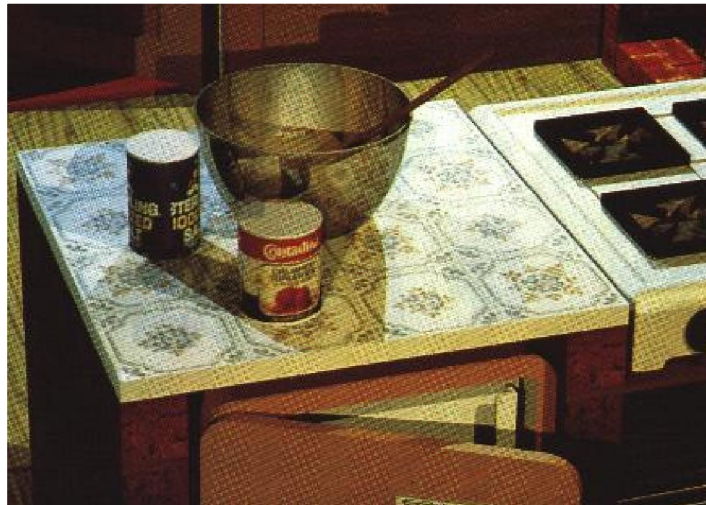
## Texture Mapping & Ray Tracing [1]: Applying Surface Detail

- Using texture maps
  - \* Add surface detail
  - \* Think of it like texturing in OpenGL
- Diffuse, specular colors
- Shininess value
- Bump map
- Transparency value

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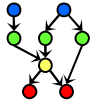
## Texture Mapping & Ray Tracing [2]: Example



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51



## Parametric Surfaces

- More expressive than triangle
- Intersection is probably slower
- $u$  and  $v$  on surface can be used as texture  $s, t$

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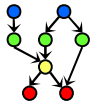
CIS 536/636

Introduction to Computer Graphics

Lecture 31 of 41

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52



## Constructive Solid Geometry

- Union, Subtraction, Intersection of solid objects
- Have to keep track of intersections



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CIS 536/636

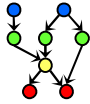
Introduction to Computer Graphics

Lecture 31 of 41

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53



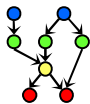
## Hierarchical Transformation

- Scene made of parts
- Each part made of smaller parts
- Each smaller part has transformation linking it to larger part
- Transformation can change over time: animation (CGA)

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54

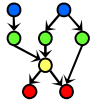


## Distributed Ray Tracing [1]: Basic Idea

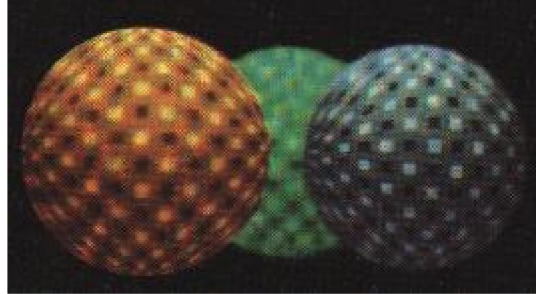
- Average multiple rays instead of just one ray
- Use for both shadows, reflections, transmission (refraction)
- Use for motion blur
- Use for depth of field

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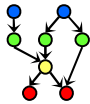




## Distributed Ray Tracing [2]: Example

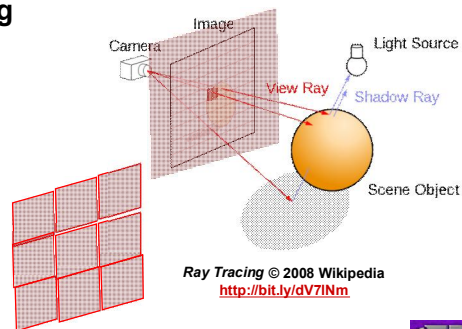


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## Distributed Ray Tracing [3]: Supersampling

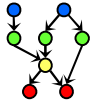
- One ray is not enough (jaggies)
- Can use multiple rays per pixel - *supersampling*
- Can use a few samples, continue if they're very different - *adaptive supersampling*
- Texture interpolation & filtering



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57



## Acceleration!

- 1280x1024 image with 10 rays/pixel
- 1000 objects (triangle, CSG, NURBS)
- 3 levels recursion

39321600000 intersection tests

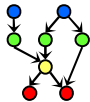
100000 tests/second -> **109 days!**

**Must use an acceleration method!**

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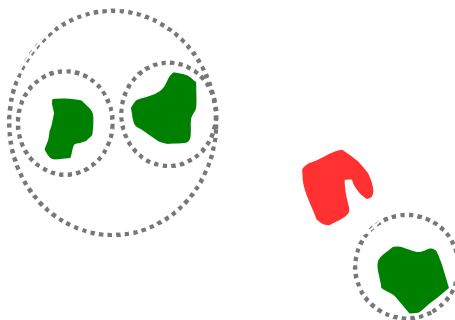


58



## Bounding Volumes

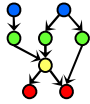
- Use simple shape for quick test, keep BV hierarchy



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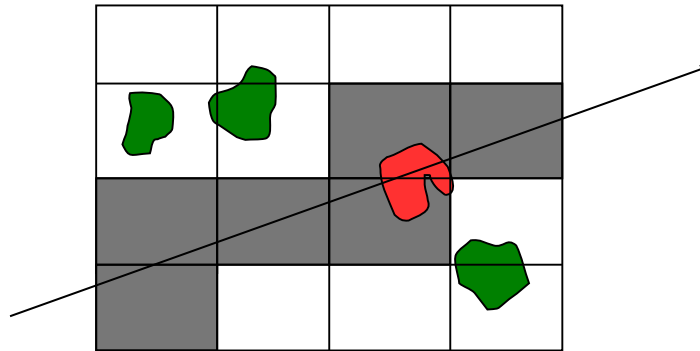


59



## Spatial Partitioning: Subdivision

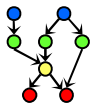
- Break your space into pieces
- Search the structure linearly



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60



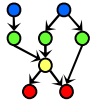
## Parallelism

- Can always throw more processors at it
- Parallel computing model
  - \* Multiple processes or threads
  - \* Data parallel: separate pixel for each

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61



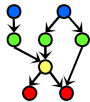
## Really Advanced Stuff

- Error analysis
- Hybrid radiosity/ray-tracing
- Metropolis Light Transport
- Memory-Coherent Ray-tracing

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62

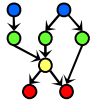


## References

- *Introduction to Ray-Tracing*, Glassner et al., 1989, 0-12-286160-4
- *Advanced Animation and Rendering Techniques*, Watt & Watt, 1992, 0-201-54412-1
- *Computer Graphics: Image Synthesis*, Joy et al., 1988, 0-8186-8854-4
- SIGGRAPH Proceedings (All)

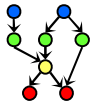
Adapted from slides ♥ 2001 D. Shreiner & B. Grantham, SCU  
COEN 290: Computer Graphics I, Winter 2001 – <http://bit.ly/hz1kfU>





## Summary

- Reading for Last Class: §5.3, Eberly 2<sup>e</sup>; **CGA Handout**
- Reading for Today: Chapter 14, Eberly 2<sup>e</sup>
- Reading for Next Class: **Ray Tracing Handout**
- Last Class: Particle Systems, Collisions, IK/CGA Concluded
  - \* Dynamics vs. kinematics, forward vs. inverse revisited
  - \* IK: autonomous vs. hand-animated; solution approaches
  - \* Rag doll physics, rigid-body dynamics, physically-based models
- Today: Ray Tracing, Part 1 of 2
  - \* **Vectors**
    - Light (L): to point light sources (or shadows)
    - Reflected (R): from object surface
    - Transmitted or Transparency (T): through transparent object
  - \*  $t_{\min}$ : distance to intersection between ray and bounding volume
  - \* Ways to find  $t_{\min}$
  - \* Basic recursive ray tracing: ray trees



## Terminology

- Joints: Parts of Robot / Articulated Figure That Turn, Slide
- Effectors: Parts of Robot / Articulated Figure That Act (e.g., Hand, Foot)
- Bones: Effectors, Other Parts That Rotate about, Slide through Joints
- Procedural Animation: Automatic Generation of Motion *via* Simulation
- Ray Tracing aka Ray Casting
  - \* Given: screen with pixels ( $u, v$ )
  - \* Find intersection  $t_{\min}(u, v)$  of rays through each ( $u, v$ ) with scene
  - \* Calculate vectors emanating from world-space coordinate of  $t_{\min}$ 
    - Light (L): to point light sources (or shadows)
    - Reflected (R): from object surface
    - Transmitted or Transparency (T): through transparent object
  - \* Recursive RT: call raytracer for each intersection found
    - Builds ray tree rooted at intersection point
    - Base cases: unobstructed vector to light; depth limit
  - \* Parallel RT: use multiple threads/processes for each ( $u, v$ ) or  $t$

