

**Lecture 12 of 41**

## Surface Detail 3 of 5: Mappings OpenGL Textures

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KSOL course pages: <http://bit.ly/hGvXIH/> / <http://bit.ly/eVizrE>  
Public mirror web site: <http://www.kddresearch.org/Courses/CIS636>  
Instructor home page: <http://www.cis.ksu.edu/~bhsu>

Readings:  
Today: Sections 20.5 – 20.13, Eberly 2<sup>e</sup> – see <http://bit.ly/ieUq45>  
Next class: Section 3.1, Eberly 2<sup>e</sup>  
Brown CS123 slides on Polygons/Texture Mapping – <http://bit.ly/h2VZn8>  
Wayback Machine archive of Brown CS123 slides: <http://bit.ly/qAhJbh>  
Gröller & Jeschke slides on Texturing – <http://bit.ly/dJFYq9>

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**Lecture Outline**

- Reading for Last Class: §2.6.3, 20.3 – 20.4, Eberly 2<sup>e</sup>
- Reading for Today: §20.5 – 20.13, Eberly 2<sup>e</sup> (Many Mappings)
- Reading for Next Class: §3.1, Eberly 2<sup>e</sup>
- Last Time: Texture Mapping Explained
  - Definitions and design principles
  - Enclosing volumes: cylinder, sphere, box
  - Mapping methods
    - reflected ray – bounce ray off object O
    - object normal – ray from face normal of object (polygon mesh)
    - object center – ray from center of object
    - intermediate surface normal – ray from inside of enclosing S
- Today: Mappings, OpenGL Texturing
  - Shadow, reflection/environment, transparency, bump, displacement
  - Other mappings: gloss, volumetric fog, skins, rainbows, water
  - OpenGL texture mapping how-to

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**Where We Are**

| Lecture | Topic  | Primary Source(s)                 |
|---------|--|-----------------------------------|
| 0       | Course Overview                              | Chapter 1, Eberly 2 <sup>e</sup>  |
| 1       | CG Basics: Transformation Matrices; Lab 0    | Sections (B) 2.1, 2.2             |
| 2       | Viewing 1: Overview, Projections             | § 2.2.3 – 2.2.4, 2.8              |
| 3       | Viewing 2: Viewing Transformation            | § 2.3 esp. 2.3.4; FVFH slides     |
| 4       | Lab 1a: Flash & OpenGL Basics                | Ch. 2, 16', Angel Primer          |
| 5       | Viewing 3: Graphics Pipeline                 | § 2.3 esp. 2.3.7; 2.6, 2.7        |
| 6       | Scan Conversion 1: Lines, Midpoint Algorithm | § 2.5.1, 3.1; FVFH slides         |
| 7       | Viewing 4: Clipping & Culling; Lab 1b        | § 2.3.5, 2.4, 3.1.3               |
| 8       | Scan Conversion 2: Polygons, Clipping Intro  | § 2.4, 2.5 esp. 2.5.4, 3.1.6      |
| 9       | Surface Detail 1: Illumination & Shading     | § 2.5, 2.6.1 – 2.6.2, 4.3.2, 20.2 |
| 10      | Lab 2a: DirectIO / DirectX Intro             | § 2.7, DirectIO handout           |
| 11      | Surface Detail 2: Textures, OpenGL Shading   | § 2.6.3, 20.3 – 20.4, Primer      |
| 12      | Surface Detail 3: Mappings, OpenGL Textures  | § 20.5 – 20.13                    |
| 13      | Surface Detail 4: Pixel/Vertex Shad.; Lab 2b | § 3.1                             |
| 14      | Surface Detail 5: DirectIO Shading; DirectIO | § 3.2 – 3.4, DirectIO handout     |
| 15      | § 4.1 – 4.3, CGA handout                     |                                   |
| 16      | Lab 3a: Shading & Transparency               | § 2.6, 20.1, Primer               |
| 17      | Animation 1: Basics, Keyframes; HW/Exam      | § 5.1 – 5.2                       |
| 18      | Exam 1 review: Hour Exam 1 (evening)         | Chapters 1 – 4, 20                |
| 19      | Scene Graphics: Rendering; Lab 3b: Shader    | § 4.4 – 4.7                       |
| 20      | Demos 2: SFX: Skinning, Morphing             | § 6.3 – 6.5, CGA handout          |
| 20      | Demos 3: Surfaces/Volume-Graphics            | § 10.4, 12.7, Mesh handout        |

Lightly-shaded entries denote the due date of a written problem set; heavily-shaded entries, that of a machine problem (programming assignment); blue-shaded entries, that of a paper review; and the green-shaded entry, that of the term project.  
Green, blue and red letters denote exam review, exam, and exam solution review dates.

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**Review: OpenGL Shading (Overview)**

- Set Up Point Light Sources
  - Directional light given by "position" vector  

```
GLfloat light_position[] = {1.0, 1.0, -1.0, 0.0};
glLightfv(GL_LIGHT0, GL_POSITION, light_position);
```
  - Point source given by "position" point  

```
GLfloat light_position[] = {1.0, 1.0, -1.0, 1.0};
glLightfv(GL_LIGHT0, GL_POSITION, light_position);
```
- Set Up Materials, Turn Lights On
  - ```
GLfloat mat_specular[] = {0.0, 0.0, 0.0, 1.0};
GLfloat mat_diffuse[] = {0.8, 0.6, 0.4, 1.0};
GLfloat mat_ambient[] = {0.8, 0.6, 0.4, 1.0};
GLfloat mat_shininess[] = {20.0};
glMaterialfv(GL_FRONT, GL_SPECULAR, mat_specular);
glMaterialfv(GL_FRONT, GL_AMBIENT, mat_ambient);
glMaterialfv(GL_FRONT, GL_DIFFUSE, mat_diffuse);
glMaterialf(GL_FRONT, GL_SHININESS, mat_shininess);
glShadeModel(GL_SMOOTH); /*enable smooth shading */
glEnable(GL_LIGHTING); /* enable lighting */
glEnable(GL_LIGHT0); /* enable light 0 */
```
- Start Drawing (glBegin ... glEnd)

Frank Pfenning  
Professor of Computer Science  
School of Computer Science  
Carnegie Mellon University  
<http://www.cs.cmu.edu/~fp/>

See also: *OpenGL: A Primer*, 3<sup>e</sup> (Angel)  
<http://bit.ly/hVcVWN>

Adapted from slides © 2003 F. Pfenning, Carnegie Mellon University  
<http://bit.ly/g1J2nj>

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**Acknowledgements: Many Mappings**



**Stefan Jeschke**  
Research Assistant  
<http://bit.ly/hUUM94>



**Eduard Gröller**  
Associate Professor  
Director, Visualization Working Group  
<http://bit.ly/hUUM94>

Institute of Computer Graphics and Algorithms  
Technical University of Vienna

Texturing material from slides © 2002 E. Gröller & S. Jeschke, Vienna University of Technology  
<http://bit.ly/dJFYq9>



Mapping material from slides © 1995 – 2009 P. Hanrahan, Stanford University  
<http://bit.ly/hZfsjz>, (CS 348B, Computer Graphics: Image Synthesis Techniques)

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**Overview of Mappings: Eberly 2<sup>e</sup> Chapter 20 Sections**

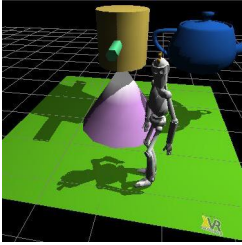
- Fine Surface Detail: Bump (§20.5 Eberly 2<sup>e</sup>)
- Material Effects: Gloss (§20.6)
- Enclosing Volumes
  - Sphere (§20.7)
  - Cube (§20.8)
- Light
  - Refraction for Transparency (§20.9)
  - Reflection aka Environment (§20.10)
- Shadow
  - Shadow Maps (§20.11, 20.13)
  - Projective Textures (§20.12)
- More Special Effects (SFX)
  - Fog (§20.14)
  - Skinning (§20.15)
  - Iridescence (§20.16), Water (§20.17)

Babylon 5  
© 1993 – 1998 Warner Brothers Entertainment, Inc.

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## Shadow Mapping [1]: Basic Concept

- Process for Adding Shadows in 3-D CG
- Compatible with Local Illumination
  - Global method: [shadow rays](#)
  - Not needed here as in raytracing
  - Instead, use [decaling](#)
- Decals
  - "Paste" surface detail onto model
  - Semi-transparent: alpha blending
  - Can simulate many attributes



Shadow Mapping © 2007 XVR Wiki  
[http://wiki.vrmedia.it/index.php?title=Shadow\\_Mapping](http://wiki.vrmedia.it/index.php?title=Shadow_Mapping)

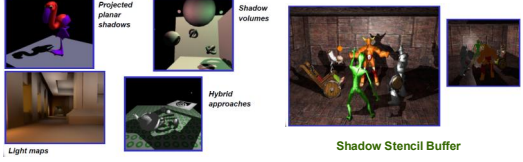
Shadow Mapping © 2005 Wikipedia  
[http://en.wikipedia.org/wiki/Shadow\\_mapping](http://en.wikipedia.org/wiki/Shadow_mapping)

Without shadow map      With shadow map

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## Shadow Mapping [2]: Techniques

- Ways to Handle Shadows
  - Projected planar shadows: works well on flat surfaces only
  - Shadow stencil buffer: powerful, excellent results possible; hard!



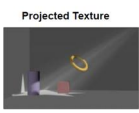
- OpenGL Shadow Mapping Tutorials
  - Beginner/Intermediate (Baker, 2003): <http://bit.ly/e1LA2N>
  - Advanced (Octavian et al., 2000): <http://bit.ly/f1iRYB> (old NeHe #27)

Adapted from "Shadow Mapping" © 2001 C. Everitt, nVidia  
[http://developer.nvidia.com/object/shadow\\_mapping.html](http://developer.nvidia.com/object/shadow_mapping.html)

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## Shadow Mapping [3]: Advanced Methods & Research

- Shadow Mattes (Hanrahan)
 



```

        UberLight ( )
        {
            Clip to near/far planes
            Clip to shape boundary
            foreach superelliptical blocker
                atten *= ...
            foreach cookie texture
                atten *= ...
            foreach slide texture
                color *= ...
            foreach noise texture
                atten, color *= ...
            foreach shadow map
                atten, color *= ...
            Calculate intensity fall-off
            Calculate beam distribution
        }
      
```



- Can Be Layered (See Maya 2011 Tutorial by Maciek Gryka)

Adapted from slides © 1995 – 2009 P. Hanrahan, Stanford University  
<http://bit.ly/hZfsjZ> (CS 348B)

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## Reflection/Environment Mapping [1]: Basic Concept

- Reflection Maps (Special Type) ~ Environment Maps (General Case)
  - For a given viewing direction
    - For each normal direction
      - Evaluate reflection equation
- Idea: Take Picture of Scene Faced by Object, Apply as Map to Object
- Requirements: Need to Take Account of Projective Distortions




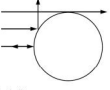
Ray Traced      Environment Map

Adapted from slides © 1995 – 2009 P. Hanrahan, Stanford University  
<http://bit.ly/hZfsjZ> (CS 348B)

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## Reflection/Environment Mapping [2]: Techniques

- Gazing Ball (Mirrorball)
 



- Reflection Functions
  - Diffuse: irradiance map
  - Glossy: radiance map
  - Anisotropic: for each tangent direction
  - Mirror: reflection map (related to environment map)
- Illumination Functions: Environment Map or Procedural Light Sources

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## Reflection/Environment Mapping [3]: Advanced Methods & Research

- How To Create Direction Maps
  - Latitude-Longitude (Map Projections) - paint
  - Gazing Ball - photograph reflective sphere
  - Fisheye Lens - standard (wide-angle) camera lens
  - Cubical Environment Map - rendering program or photography
    - Easy to produce
    - "Uniform" resolution
    - Simple texture coordinates calculation
- Old NeHe OpenGL Mapping Tutorials (2000)
  - #6 (texture map onto cube) – Beginner (Molofeev): <http://bit.ly/gKj2Nb>
  - #23 (sphere) – Intermediate (Schmick & Molofeev): <http://bit.ly/e3Zb8h>
- nVidia Tutorial: OpenGL Cube Map (1999): <http://bit.ly/eJEdAM>
- Issues: Non-Linear Mapping, Area Distortion, Converting Between Maps


Adapted from slides © 1995 – 2009 P. Hanrahan, Stanford University  
<http://bit.ly/hZfsjZ> (CS 348B)

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## Transparency Mapping [1]: Basic Concept

- **Transparency: One Term for Many Techniques**  
Tom Porter's Bowling Pin



Source: RenderMan Companion, Pls. 12 & 13

- **Goal: "See Through" Objects (Could Be Real Decals)**
- **Ideas: Render Background Object, Then Foreground Object or Material**
  - \* Blend in color of (semi-)transparent/translucent foreground object
  - \* Simulate little holes in foreground material (screen door)

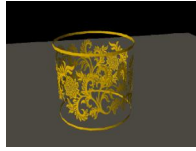
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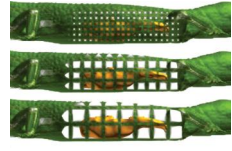
14

## Transparency Mapping [2]: Techniques

- **Alpha Compositing aka Alpha Blending**
  - \* Combine colors of transparent foreground, opaque background
  - \* Uses **alpha channel A** of (R, G, B, A) – think “% transparency”
  - \* Wikipedia: <http://bit.ly/ePpwoh> (see also RGBA, <http://bit.ly/ePpwoh>)



Alpha blending: Lim (2010), <http://bit.ly/STaJrb>  
Goon Creative, Maya Transparency Tutorial



Screen door: Viola et al. (2004), <http://bit.ly/dVYa7I>  
Technical University of Vienna, IEEE Vis 2004

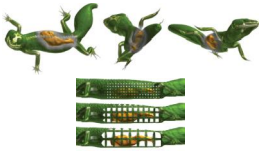
- **Screen Door Transparency**
  - \* Simulate little holes in foreground material (screen door)
  - \* Result: visual effect of being able to see through foreground

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## Transparency Mapping [3]: Advanced Methods & Research

- OpenGL Transparency How-To at [OpenGL.org](http://bit.ly/hRaQgk): <http://bit.ly/hRaQgk>
- Screen Door Transparency
  - \* Use `glPolygonStipple()`, `glEnable(GL_POLYGON_STIPPLE)`
  - \* See <http://bit.ly/g1hQpJ>
- Glass-Like Transparency using Alpha Blending
  - \* Use `glEnable(GL_BLEND)`, `glBlendFunc(...)`
  - \* See <http://bit.ly/hs82Za>



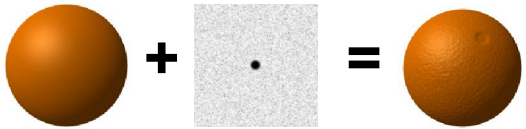
Viola et al. (2004), <http://bit.ly/dVYa7I>  
Technical University of Vienna, IEEE Vis 2004

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## Bump Mapping [1]: Basic Concept

- **Goal: Create Illusion of Textured Surface**




Bump Mapping © 2010 Wikipedia  
[http://en.wikipedia.org/wiki/Bump\\_mapping](http://en.wikipedia.org/wiki/Bump_mapping)

- **Idea**
  - \* Start with regular smooth object
  - \* Make height map (by hand and/or using program, i.e., procedurally)
  - \* Use map to perturb surface normals
  - \* Plug new normals into illumination equation
- Will This Look Realistic? Why/Why Not?

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## Bump Mapping [2]: Techniques



$$\mathbf{P}(u,v)$$

$$\mathbf{S}(u,v) = \frac{\partial \mathbf{P}(u,v)}{\partial u} \quad \mathbf{T}(u,v) = \frac{\partial \mathbf{P}(u,v)}{\partial v}$$

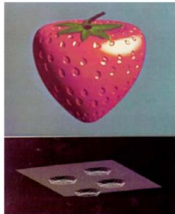
$$\mathbf{N}(u,v) = \mathbf{S} \times \mathbf{T}$$

- **Displacement**  

$$\mathbf{P}'(u,v) = \mathbf{P}(u,v) + h(u,v)\mathbf{N}(u,v)$$
- **Perturbed normal**  

$$\mathbf{N}'(u,v) = \mathbf{P}'_u \times \mathbf{P}'_v$$

$$= \mathbf{N} + h_u(\mathbf{T} \times \mathbf{N}) + h_v(\mathbf{S} \times \mathbf{N})$$



From Blinn 1976

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<http://bit.ly/hZfsjZ> (CS 348B)

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## Bump Mapping [3]: Advanced Methods & Research

- Bump Mapping Tutorial for OpenGL (Baker, 2003): <http://bit.ly/fun4a5>



Hey, wait a minute!



... what's wrong with the one on the left?

- Right Ball (Displacement Mapped) Casts **Rough** Shadow
- Left Ball (Bump Mapped) Casts **Smooth** Shadow – Why?
- Bump Mapping Only Perturbs Normals (Surface Only!)

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## Displacement Mapping [1]: Basic Concept

- Remember What We Did to Perform Bump Mapping?

$$\mathbf{P}(u,v)$$

$$\mathbf{S}(u,v) = \frac{\partial \mathbf{P}(u,v)}{\partial u} \quad \mathbf{T}(u,v) = \frac{\partial \mathbf{P}(u,v)}{\partial v}$$

$$\mathbf{N}(u,v) = \mathbf{S} \times \mathbf{T}$$

- Displacement

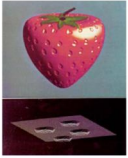
$$\mathbf{P}'(u,v) = \mathbf{P}(u,v) + h(u,v)\mathbf{N}(u,v)$$

- Perturbed normal

$$\mathbf{N}'(u,v) = \mathbf{P}'_u \times \mathbf{P}'_v$$

$$= \mathbf{N} + h_u(\mathbf{T} \times \mathbf{N}) + h_v(\mathbf{S} \times \mathbf{N})$$

From Blinn 1976




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## Displacement Mapping [2]: Techniques

- Displacement Map: Similar to Bump Map – Contains Delta Values



Displacement Mapping © 2005 Wikipedia  
[http://en.wikipedia.org/wiki/Displacement\\_mapping](http://en.wikipedia.org/wiki/Displacement_mapping)

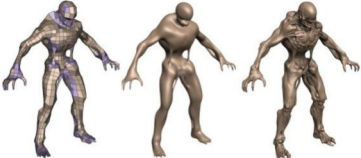
- Displacement Mapping: Uses Open GL Shading Language (GLSL)
- Tutorial using GLSL (Guinot, 2006): <http://bit.ly/dWXNya>

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## Displacement Mapping [3]: Advanced Methods & Research

- When To Consider Using Displacement Mapping
  - Very “deep” texture effect: veins, ridges, etc.
  - Shadows expected




The “Imp” © 2008 K. Scott, id Software 2008  
 The “Imp” © 2008 K. Scott, id Software  
 Bjorn3D, <http://bit.ly/i78SiP>

Like Many Mappings and Other Effects, Wanted In Hardware!


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## Acknowledgements: Texture Mapping Slides



Andy van Dam  
 T. J. Watson University Professor of Technology and Education & Professor of Computer Science  
 Brown University  
<http://www.cs.brown.edu/~avd/>



### Texture Mapping

Beautification of Surfaces

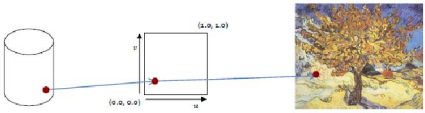
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## Texture Mapping Technique [1]

- Texture mapping is the process of mapping a geometric point in space to a value (color, normal, other...) in a texture
- Our goal is to map any arbitrary geometry to a texture of any dimension
- This is done in two steps:
  - Map a point on the geometry to a point on the unit square
  - Map the unit square point to point on the texture



Van Gogh

Second mapping is much easier, we'll present it first.

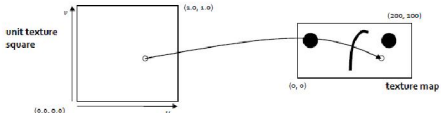
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## Texture Mapping Technique [2]

- Mapping a point in the unit  $u, v$  square to a texture of arbitrary dimension:
  - In general, any point  $(u, v)$  on the unit square, the corresponding point on the texture of length  $l$  pixels and height  $h$  pixels is  $(u * l, v * h)$ .



- Above:  $(0,0,0,0) \rightarrow (0,0)$ ;  $(1,0,1,0) \rightarrow (200,100)$ ;  $(.7, .45) \rightarrow (140,45)$
- Once we have coordinates for the texture, we just need to look up the color of the texture at these coordinates
- Coordinates not always a discrete point on texture as they come from continuous space. May need to average neighboring texture pixels (i.e. filter)

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## Texture Mapping Technique [3]

- Texture mapping polygons
  - $(u, v)$  texture coordinates are pre-calculated and specified per vertex
  - Vertices may have different texture coordinates for different faces

Texture coordinates are linearly interpolated across polygon

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## Interpolation Trick: Barycentric Coordinates

- Consider interpolating between two values along a line
  - Given two colors  $C_a$  and  $C_b$ , you can compute any value along the "line" between the two colors by evaluating:
 
$$C(t) = (1-t)C_a + tC_b \quad 0 \leq t \leq 1$$
  - This equation can be written as:
 
$$C(s, t) = sC_a + tC_b \quad s + t = 1 \quad s, t \geq 0$$
  - $s$  and  $t$  are the Barycentric Coordinates of the line segment between  $C_a$  and  $C_b$
  - The EQ of the line is a convex linear combination of its endpoints. We've seen this before (splines, color theory)
- Barycentric coordinates can be generalized to triangles
 
$$C(s, t, u) = sC_a + tC_b + uC_c \quad s + t + u = 1 \quad s, t, u \geq 0$$

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## Applying Barycentric Coordinates

- When you intersect a ray with a polyhedral object (not needed for our intersect/ray projects):
  - return the vertex data of the triangle intersected
  - return the Barycentric coordinates  $(t_1, t_2, t_3)$  of the intersection point
  - These coordinates can be used to interpolate between vertex colors, normals, texture coordinates, or other data
  - What weights do we hang on each vertex such that the triangle would be perfectly balanced on a pin at point  $P$
  - Alternatively, think of a mobile suspended from  $P$  with 2 arms  $A_1Q$  and  $A_2A_3$ .
  - Compute  $Q$  as intersection of line through  $A_1$  and  $P$  and line through  $A_2$  and  $A_3$
  - $t_2' = |Q - A_2|$
  - $t_3' = |Q - A_3|$
  - $t_1' = |P - Q|$
  - $(t_1, t_2, t_3) = (t_1', t_2', t_3') / (t_1' + t_2' + t_3')$
  - Another way of thinking about this is by triangle area. The weight at  $A_1$  should be proportional to the area of the triangle  $P, A_2, A_3$ , and so on...

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## Texture Mapping Technique [4]: Map Point to Object on $(u, v)$ Square

- Texture mapping in "Ray": mapping solids
  - Using ray tracing, we obtain an intersection point  $(x, y, z)$  in object space
  - We need to map this point to a point on the  $(u, v)$  unit square, so we can map that to a texture value
  - Three easy cases: planes, cylinders, and spheres
- Easiest to compute the mapping from  $(x, y, z)$  coordinates in object space to  $(u, v)$
- Can cause unwanted texture scaling
- Texture filtering is an option in most graphics libraries
- OpenGL allows you to choose filtering method. (GL\_NEAREST, GL\_LINEAR, etc...)

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## Texture Mapping Technique [5]

- Texture mapping large quads:
  - How to map a point on a very large quad to a point on the unit square?
  - Tiling: texture is repeated over and over across infinite plane
  - Given coordinates  $(x, y)$  of a point on an arbitrarily large quad to tile with quads of size  $(w, h)$ , the  $(u, v)$  coordinates on the unit square representing a texture with arbitrary dimensions are:
 
$$(u, v) = \left( \frac{x \% w}{w}, \frac{y \% h}{h} \right)$$

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## Texture Mapping Technique [6]

- How to texture map cylinders and cones:
  - Given a point  $P$  on the surface:
    - If it's on one of the caps, map as though the cap is a plane
    - If it's on the curved surface:
      - Use the position of the point around the perimeter to determine  $u$
      - Use the height of the point to determine  $v$
- Mapping  $v$  is trivial,  $[-.5, .5]$  gets mapped to  $[0.0, 1.0]$  just by adding .5

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## Texture Mapping Technique [7]

- Computing the  $u$  coordinate for cones and cylinders:
  - We need to map all the points on the perimeter of the object to  $[0, 1]$ .
  - The easiest way is to say  $u = \frac{\theta}{2\pi}$ , but computing  $\theta$  can be tricky

$\theta = \pi/2 \quad u = 0.25$   
 $\theta = \pi \quad u = 0.5$   
 $\theta = 3\pi/2 \quad u = 0.75$   
 $\theta = 2\pi \quad u = 1.0$

Note: arrows point in the direction of increasing  $u$ , not  $\theta$

- Standard atan function computes a result for  $\theta$  but its always between 0 and  $\pi$  and it maps two positions on the perimeter to the same  $\theta$  value.
  - Example:  $\text{atan}(1, 1) = \text{atan}(-1, -1) = \frac{\pi}{4}$
- $\text{atan2}(x, y)$  yields values between  $-\pi$  and  $\pi$ , but isn't continuous. See above diagram.

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## Texture Mapping Technique [8]

- Texture mapping spheres:
  - Find  $(u, v)$  coordinates for P
  - We compute  $u$  the same we do for cylinders and cones
  - If  $v = 0$  or  $v = 1$ , there is a singularity. Set  $u$  to some predefined value. ( $\xi$  is good)
  - $v$  is a function of the latitude of P

$u = \text{longitude}$   
 $v = \text{latitude}$

$$\phi = \sin^{-1} \frac{P_y}{r} \quad -\frac{\pi}{2} \leq \phi < \frac{\pi}{2} \quad r = \text{radius}$$

$$v = \frac{\phi}{\pi} + .5$$

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## Texture Mapping Style [1]: Tiling

- We want to create a brick wall with a brick pattern texture
  - A brick pattern is very repetitive, we can use a small texture and "tile" it across the wall

Texture

Without Tiling

With Tiling

- Tiling allows you to scale repetitive textures to make texture elements just the right size.

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## Texture Mapping Style [2]: Stretching

- With non-repetitive textures, we have less flexibility
  - Have to fill an arbitrarily large object with a texture of finite size
  - Can't tile, have to stretch
- Example, creating a sky backdrop:
 

Texture

Applied with stretching

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## Texture Mapping Complex Geometry [1]

- Sometimes, reducing objects to primitives for texture mapping doesn't achieve the right result.
  - Consider a simple house shape as an example
  - If we texture map it by our old methods, we get discontinuities at some edges.

- Solution: Pretend object is a sphere and texture map using the sphere  $(u, v)$  map

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## Texture Mapping Complex Geometry [2]

- Intuitive approach: Place a bounding sphere around the complex object
  - Find ray's object space intersection with bounding sphere
  - Convert to  $(u, v)$  coordinates

Stage one: intersect ray with bounding sphere

Stage two: calculate intersection point's  $u-v$  coords

- We actually don't need a bounding sphere!
  - Once we have the intersection point with the object, we just treat it as though it were on the sphere. Same results, but be careful with radii.

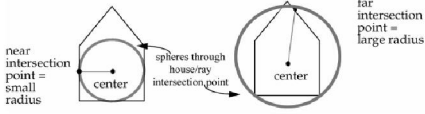
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## Texture Mapping Complex Geometry [3]

- When we treat the object intersection point as a point on a sphere, our "sphere" won't always have the same radius




- What radius to use?
  - Compute the radius as the distance from the center of the complex object to the intersection point. Use that as the radius for the  $(u, v)$  mapping.


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## Texture Mapping Complex Geometry [4]

- Results of spherical  $(u, v)$  mapping:
 
- You can use cylindrical or planar mappings for complex objects as well
  - Each has drawbacks
    - Spherical: warping at the "poles" of the object
    - Cylindrical: discontinuities at the caps
    - Planar: one dimension must be ignored



- For best overall results, mapping techniques can be swapped

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## OpenGL Texturing [1]: Steps

- Create and specify a texture object
  - Create a texture object
  - Specify the texture image
  - Specify how texture has to be applied for each pixel
- Enable texture mapping
- Draw the textured polygons
  - Identify the active texture
  - Specify texture coordinates with vertices

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## OpenGL Texturing [2]: Specify 2-D Texture Object

- `glTexImage2D(GLenum target, GLint level, GLint internalformat, GLsizei width, GLsizei height, GLint border, GLenum format, GLenum type, const GLvoid *texels);`
  - Eg: `glTexImage2D(GL_TEXTURE_2D, 0, GL_RGBA, 128, 128, 0, GL_RGBA, GL_UNSIGNED_BYTE, image);`
  - `format` and `type` used to specify the way the texels are stored
  - `internalFormat` specifies how OpenGL should store the data internally
  - `width` and `height` have to be powers of 2; you can use `gluScaleImage()` to scale

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## OpenGL Texturing [3]: Specify How Texture Is Applied

- `glTexParameterf(GLenum target, GLenum pname, TYPE param)`
- `target` can be: `GL_TEXTURE_1D`, `GL_TEXTURE_2D`, ...

| pname                              | param                                            |
|------------------------------------|--------------------------------------------------|
| <code>GL_TEXTURE_WRAP_S</code>     | <code>GL_CLAMP</code> , <code>GL_REPEAT</code>   |
| <code>GL_TEXTURE_WRAP_T</code>     | <code>GL_CLAMP</code> , <code>GL_REPEAT</code>   |
| <code>GL_TEXTURE_MAG_FILTER</code> | <code>GL_NEAREST</code> , <code>GL_LINEAR</code> |
| <code>GL_TEXTURE_MIN_FILTER</code> | <code>GL_NEAREST</code> , <code>GL_LINEAR</code> |

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## OpenGL Texturing [4]: Enable Texture and Draw

- `glEnable(GL_TEXTURE_2D)`
  - Enable 2D texturing
- `glTexCoord2f(GL_FLOAT u, GL_FLOAT v)`
  - Specify texture coordinates per vertex (just as normals, color, etc).

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## OpenGL Texturing [5]: Create Texture Object

- **glGenTextures**(GLsizei *n*, GLuint\* *textureIDs*);
  - Returns *n* currently unused texture ID in *textureIDs*
  - Each texture ID is an integer greater than 0
- **glBindTexture**(GLenum *target*, GLuint *textureID*);
  - *target* is GL\_TEXTURE\_1D, GL\_TEXTURE\_2D, or GL\_TEXTURE\_3D
  - if *textureID* is being used for the first time a new texture object is created and assigned the ID = *textureID*
  - if *textureID* has been used before, the texture object with ID = *textureID* becomes active

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## OpenGL Texturing [6]: Putting It All Together

In initialization:

```
glGenTextures(...);
glBindTexture(...);
glTexParameteri(...); glTexParameteri(...); ...
glTexImage2D(...);
glEnable(GL_TEXTURE_2D);
```

In display:

```
glBindTexture(...); // Activate the texture defined in
// initialization
glBegin(GL_TRIANGLES);
glTexCoord2f(...); glVertex3f(...);
glTexCoord2f(...); glVertex3f(...);
glTexCoord2f(...); glVertex3f(...);
glEnd();
```

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## Preview: Texturing with Blocks

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## Preview: Mipmapping

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## Summary

- **Last Time: Texture Mapping Explained**
  - \* Definitions and design principles
  - \* Enclosing volumes: cylinder, sphere, box
  - \* Mapping methods
    - reflected ray
    - object normal
    - object center
    - intermediate surface normal
- **Today: Mappings, OpenGL Texturing**
  - \* Idea: define “texture” to simulate surface detail
  - \* Shadow, reflection/environment, transparency, bump, displacement
  - \* Other mappings: gloss, volumetric fog, skins, rainbows, water
  - \* OpenGL texture mapping how-to

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## Terminology

- **Texture Mapping - Adding Detail, Raster Image, Color, etc. to CG Model**
  - \* **Planar projection**: apply flat texture to flat surface(s)
  - \* **Enclosing volumes**: cylinder, sphere, box
  - \* **Mapping methods**
    - **reflected ray** – bounce ray off object *O*
    - **object normal** – ray from face normal of object (polygon mesh)
    - **object center** – ray from center of object
    - **intermediate surface normal** – ray from inside of enclosing *S*
- **Mappings: Apply Image or Simulated Surface Detail to Object**
  - \* **Shadow**: cast planar projective shadows or calculate volume
  - \* **Reflection/environment**: take picture of scene from “inside” object
  - \* **Transparency**: take picture of scene “behind” object; refract
  - \* **Bump**: perturb color based on height map
  - \* **Displacement**: perturb face normals, recalculate lighting

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