

## Lecture 12 of 41

# Surface Detail 3 of 5: Mappings OpenGL Textures

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KSOL course pages: <http://bit.ly/hGvXIH> / <http://bit.ly/eVizrE>

Public mirror web site: <http://www.kddresearch.org/Courses/CIS636>

Instructor home page: <http://www.cis.ksu.edu/~bhsu>

### Readings:

Today: Sections 20.5 – 20.13, Eberly 2<sup>e</sup> – see <http://bit.ly/ieUq45>

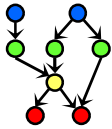
Next class: Section 3.1, Eberly 2<sup>e</sup>

Brown CS123 slides on Polygons/Texture Mapping – <http://bit.ly/h2VZn8>

Wayback Machine archive of Brown CS123 slides: <http://bit.ly/gAhJbh>

Gröller & Jeschke slides on Texturing – <http://bit.ly/dJFYq9>

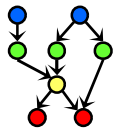




## Lecture Outline

- Reading for Last Class: §2.6.3, 20.3 – 20.4, Eberly 2<sup>e</sup>
- Reading for Today: §20.5 – 20.13, Eberly 2<sup>e</sup> (Many Mappings)
- Reading for Next Class: §3.1, Eberly 2<sup>e</sup>
- Last Time: Texture Mapping Explained
  - \* Definitions and design principles
  - \* Enclosing volumes: cylinder, sphere, box
  - \* Mapping methods
    - reflected ray – bounce ray off object  $O$
    - object normal – ray from face normal of object (polygon mesh)
    - object center – ray from center of object
    - intermediate surface normal – ray from inside of enclosing  $S$
- Today: Mappings, OpenGL Texturing
  - \* Shadow, reflection/environment, transparency, bump, displacement
  - \* Other mappings: gloss, volumetric fog, skins, rainbows, water
  - \* OpenGL texture mapping how-to





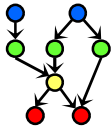
## Where We Are

Lecture	Topic	Primary Source(s)
0	Course Overview	Chapter 1, Eberly 2 <sup>e</sup>
1	<b>CG Basics: Transformation Matrices; Lab 0</b>	<b>Sections (§) 2.1, 2.2</b>
2	Viewing 1: Overview, Projections	§ 2.2.3 – 2.2.4, 2.8
3	Viewing 2: Viewing Transformation	§ 2.3 esp. 2.3.4; <a href="#">FVFH slides</a>
4	<b>Lab 1a: Flash &amp; OpenGL Basics</b>	<b>Ch. 2, 16<sup>1</sup>, <a href="#">Angel Primer</a></b>
5	Viewing 3: Graphics Pipeline	§ 2.3 esp. 2.3.7; 2.6, 2.7
6	Scan Conversion 1: Lines, Midpoint Algorithm	§ 2.5.1, 3.1; <a href="#">FVFH slides</a>
7	<b>Viewing 4: Clipping &amp; Culling; Lab 1b</b>	<b>§ 2.3.5, 2.4, 3.1.3</b>
8	Scan Conversion 2: Polygons, Clipping Intro	§ 2.4, 2.5 esp. 2.5.4, 3.1.6
9	Surface Detail 1: Illumination & Shading	§ 2.5, 2.6.1 – 2.6.2, 4.3.2, 20.2
10	<b>Lab 2a: Direct3D / DirectX Intro</b>	<b>§ 2.7, <a href="#">Direct3D handout</a></b>
11	Surface Detail 2: Textures; OpenGL Shading	§ 2.6.3, 20.3 – 20.4, <a href="#">Primer</a>
12	Surface Detail 3: Mappings; OpenGL Textures	§ 20.5 – 20.13
13	<b>Surface Detail 4: Pixel/Vertex Shad.; Lab 2b</b>	<b>§ 3.1</b>
14	Surface Detail 5: Direct3D Shading; OGLSL	§ 3.2 – 3.4, <a href="#">Direct3D handout</a>
15	Demos 1: CGA, Fun; Scene Graphs: State	§ 4.1 – 4.3, <a href="#">CGA handout</a>
16	<b>Lab 3a: Shading &amp; Transparency</b>	<b>§ 2.6, 20.1, <a href="#">Primer</a></b>
17	<b>Animation 1: Basics, Keyframes; HW/Exam</b>	<b>§ 5.1 – 5.2</b>
	<b>Exam 1 review; Hour Exam 1 (evening)</b>	<b>Chapters 1 – 4, 20</b>
18	<b>Scene Graphs: Rendering; Lab 3b: Shader</b>	<b>§ 4.4 – 4.7</b>
19	<b>Demos 2: SFX; Skinning, Morphing</b>	<b>§ 5.3 – 5.5, <a href="#">CGA handout</a></b>
20	Demos 3: Surfaces; B-reps/Volume Graphics	§ 10.4, 12.7, <a href="#">Mesh handout</a>

Lightly-shaded entries denote the due date of a written problem set; heavily-shaded entries, that of a machine problem (programming assignment); blue-shaded entries, that of a paper review; and the green-shaded entry, that of the term project.

Green, blue and red letters denote exam review, exam, and exam solution review dates.





### Frank Pfenning

Professor of Computer Science  
School of Computer Science  
Carnegie Mellon University  
<http://www.cs.cmu.edu/~fp/>

See also: *OpenGL: A Primer, 3<sup>e</sup> (Angel)*  
<http://bit.ly/hVcVWN>

Adapted from slides © 2003 F. Pfenning, Carnegie Mellon University  
<http://bit.ly/g1J2nj>

## Review: OpenGL Shading (Overview)

### ● Set Up Point Light Sources

- Directional light given by "position" **vector**  

```
GLfloat light_position[] = {-1.0, 1.0, -1.0, 0.0};
glLightfv(GL_LIGHT0, GL_POSITION, light_position);
```
- Point source given by "position" **point**  

```
GLfloat light_position[] = {-1.0, 1.0, -1.0, 1.0};
glLightfv(GL_LIGHT0, GL_POSITION, light_position);
```

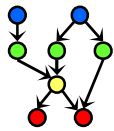
### ● Set Up Materials, Turn Lights On

```
GLfloat mat_specular[]={0.0, 0.0, 0.0, 1.0};
GLfloat mat_diffuse[]={0.8, 0.6, 0.4, 1.0};
GLfloat mat_ambient[]={0.8, 0.6, 0.4, 1.0};
GLfloat mat_shininess={20.0};
glMaterialfv(GL_FRONT, GL_SPECULAR, mat_specular);
glMaterialfv(GL_FRONT, GL_AMBIENT, mat_ambient);
glMaterialfv(GL_FRONT, GL_DIFFUSE, mat_diffuse);
glMaterialf(GL_FRONT, GL_SHININESS, mat_shininess);

glShadeModel(GL_SMOOTH); /*enable smooth shading */
glEnable(GL_LIGHTING); /* enable lighting */
glEnable(GL_LIGHT0); /* enable light 0 */
```

### ● Start Drawing (glBegin ... glEnd)





## Acknowledgements: Many Mappings



**Stefan Jeschke**

Research Assistant  
<http://bit.ly/hUUM94>

**Eduard Gröller**

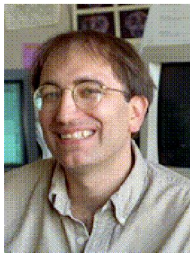
Associate Professor  
Director, Visualization Working Group  
<http://bit.ly/hUUM94>



Institute of Computer Graphics and Algorithms  
Technical University of Vienna

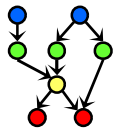


Texturing material from slides © 2002 E. Gröller & S. Jeschke, Vienna University of Technology  
<http://bit.ly/dJFYq9>



Mapping material from slides © 1995 – 2009 P. Hanrahan, Stanford University  
<http://bit.ly/hZfsjZ> (CS 348B, Computer Graphics: Image Synthesis Techniques)





## Overview of Mappings: Eberly 2<sup>e</sup> Chapter 20 Sections

- Fine Surface Detail: Bump (§20.5 Eberly 2<sup>e</sup>)
- Material Effects: Gloss (§20.6)
- Enclosing Volumes
  - \* Sphere (§20.7)
  - \* Cube (§20.8)
- Light
  - \* Refraction for Transparency (§20.9)
  - \* Reflection aka Environment (§20.10)
- Shadow
  - \* Shadow Maps (§20.11, 20.13)
  - \* Projective Textures (§20.12)
- More Special Effects (SFX)
  - \* Fog (§20.14)
  - \* Skinning (§20.15)
  - \* Iridescence (§20.16), Water (§20.17)

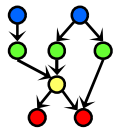


Babylon 5

© 1993 – 1998 Warner Brothers Entertainment, Inc.

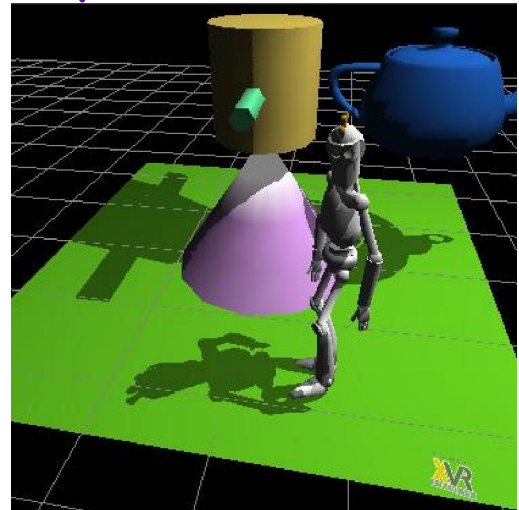






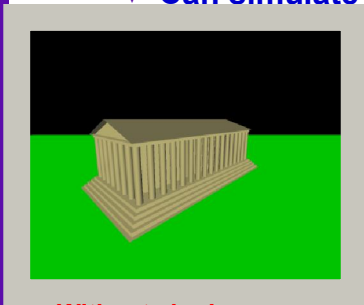
## Shadow Mapping [1]: Basic Concept

- Process for Adding Shadows in 3-D CG
- Compatible with Local Illumination
  - ✦ Global method: shadow rays
  - ✦ Not needed here as in raytracing
  - ✦ Instead, use decals
- Decals
  - ✦ “Paste” surface detail onto model
  - ✦ Semi-transparent: alpha blending
  - ✦ Can simulate many attributes

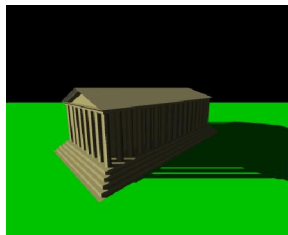


Shadow Mapping © 2007 XVR Wiki

[http://wiki.vrmedia.it/index.php?title=Shadow\\_Mapping](http://wiki.vrmedia.it/index.php?title=Shadow_Mapping)



Without shadow map

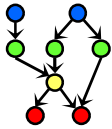


With shadow map

Shadow Mapping © 2005 Wikipedia

[http://en.wikipedia.org/wiki/Shadow\\_mapping](http://en.wikipedia.org/wiki/Shadow_mapping)





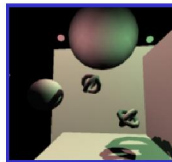
## Shadow Mapping [2]: Techniques

### ● Ways to Handle Shadows

- ✦ Projected planar shadows: works well on flat surfaces only
- ✦ Shadow stencil buffer: powerful, excellent results possible; hard!



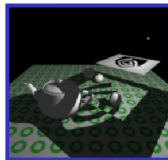
Projected  
planar  
shadows



Shadow  
volumes



Light maps



Hybrid  
approaches



Shadow Stencil Buffer

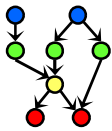
### ● OpenGL Shadow Mapping Tutorials

- ✦ Beginner/Intermediate (Baker, 2003): <http://bit.ly/e1LA2N>
- ✦ Advanced (Octavian et al., 2000): <http://bit.ly/f1iRYB> (old NeHe #27)

Adapted from "Shadow Mapping" © 2001 C. Everitt, nVidia  
[http://developer.nvidia.com/object/shadow\\_mapping.html](http://developer.nvidia.com/object/shadow_mapping.html)



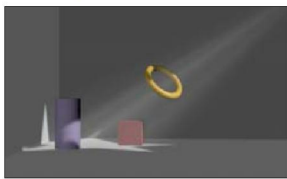




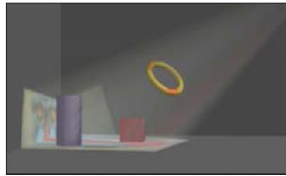
## Shadow Mapping [3]: Advanced Methods & Research

- **Shadow Mattes (Hanrahan)**

Projected Texture



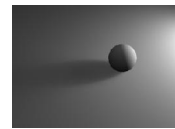
Shadow Matte



```

UberLight( )
{
  Clip to near/far planes
  Clip to shape boundary
  foreach superelliptical blocker
    atten *= ...
  foreach cookie texture
    atten *= ...
  foreach slide texture
    color *= ...
  foreach noise texture
    atten, color *= ...
  foreach shadow map
    atten, color *= ...
  Calculate intensity fall-off
  Calculate beam distribution
}

```

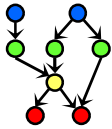


© 2010 M. Gryka  
<http://bit.ly/hJlfps>

- **Can Be Layered (See Maya 2011 Tutorial by Maciek Gryka)**

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## Reflection/Environment Mapping [1]: Basic Concept

- **Reflection Maps (Special Type) ~ Environment Maps (General Case)**
  - \* For a given viewing direction
  - \* For each normal direction
    - \* For each incoming direction (hemispherical integral)
    - \* Evaluate reflection equation
- **Idea: Take Picture of Scene Faced by Object, Apply as Map to Object**
- **Requirements: Need to Take Account of Projective Distortions**



Ray Traced

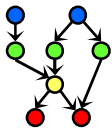


Environment Map

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<http://bit.ly/hZfsjZ> (CS 348B)





## Reflection/Environment Mapping [2]: Techniques

### ● Gazing Ball (Mirrorball)

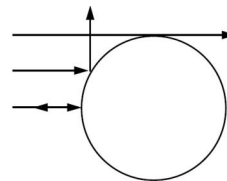
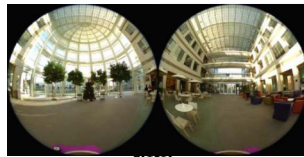


Photo © 2009 K. Turkowski

Note:

- Photograph of reflective ball
- Reflection indexed by normal
- Maps entire field of view to circle
- Resolution function of orientation; maximum head-on
- Fish eye camera lens similar

### ● Reflection Functions

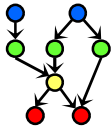
- ✧ Diffuse: irradiance map
- ✧ Glossy: radiance map
- ✧ Anisotropic: for each tangent direction
- ✧ Mirror: reflection map (related to environment map)

### ● Illumination Functions: Environment Map or Procedural Light Sources

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<http://bit.ly/hZfsjZ> (CS 348B)

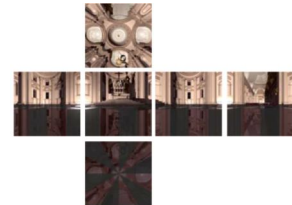




## Reflection/Environment Mapping [3]: Advanced Methods & Research

- **How To Create Direction Maps**

- \* Latitude-Longitude (Map Projections) - paint
- \* Gazing Ball - photograph reflective sphere
- \* Fisheye Lens - standard (wide-angle) camera lens
- \* Cubical Environment Map - rendering program or photography
  - Easy to produce
  - "Uniform" resolution
  - Simple texture coordinates calculation



- **Old NeHe OpenGL Mapping Tutorials (2000)**

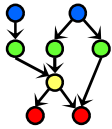
- \* #6 (texture map onto cube) – Beginner (Molofee): <http://bit.ly/gKj2Nb>
- \* #23 (sphere) – Intermediate (Schmick & Molofee): <http://bit.ly/e3Zb8h>

- **nVidia Tutorial: OpenGL Cube Map (1999):** <http://bit.ly/eJEdAM>

- **Issues: Non-Linear Mapping, Area Distortion, Converting Between Maps**

Adapted from slides © 1995 – 2009 P. Hanrahan, Stanford University  
<http://bit.ly/hZfsjZ> (CS 348B)





## Transparency Mapping [1]: Basic Concept

- **Transparency: One Term for Many Techniques**

Tom Porter's Bowling Pin



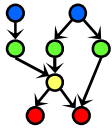
Source: RenderMan Companion, Pls. 12 & 13

- **Goal: "See Through" Objects (Could Be Real Decals)**
- **Ideas: Render Background Object, Then Foreground Object or Material**
  - ✦ Blend in color of (semi-)transparent/translucent foreground object
  - ✦ Simulate little holes in foreground material (screen door)

Adapted from slides © 1995 – 2009 P. Hanrahan, Stanford University

<http://bit.ly/hZfsjZ> (CS 348B)

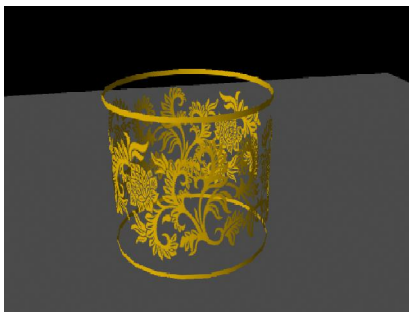




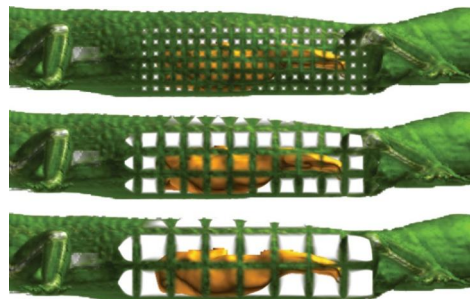
## Transparency Mapping [2]: Techniques

- **Alpha Compositing aka Alpha Blending**

- ✦ Combine colors of transparent foreground, opaque background
- ✦ Uses alpha channel A of (R, G, B, A) – think “% transparency”
- ✦ Wikipedia: <http://bit.ly/ePpwoh> (see also RGBA, <http://bit.ly/ePpwoh>)



Alpha blending: Lim (2010), <http://bit.ly/6TsJrb>  
Goon Creative, Maya Transparency Tutorial

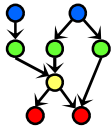


Screen door: Viola *et al.* (2004), <http://bit.ly/dVEa7I>  
Technical University of Vienna, IEEE Vis 2004

- **Screen Door Transparency**

- ✦ Simulate little holes in foreground material (screen door)
- ✦ Result: visual effect of being able to see through foreground





## Transparency Mapping [3]: Advanced Methods & Research

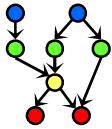
- OpenGL Transparency How-To at [OpenGL.org](http://bit.ly/hRaQgk): <http://bit.ly/hRaQgk>
- Screen Door Transparency
  - ✴ Use `glPolygonStipple()`, `glEnable(GL_POLYGON_STIPPLE)`
  - ✴ See <http://bit.ly/g1hQpJ>
- Glass-Like Transparency using Alpha Blending
  - ✴ Use `glEnable(GL_BLEND)`, `glBlendFunc(...)`
  - ✴ See <http://bit.ly/hs82Za>



Viola et al. (2004), <http://bit.ly/dVEa7I>  
Technical University of Vienna, IEEE Vis 2004

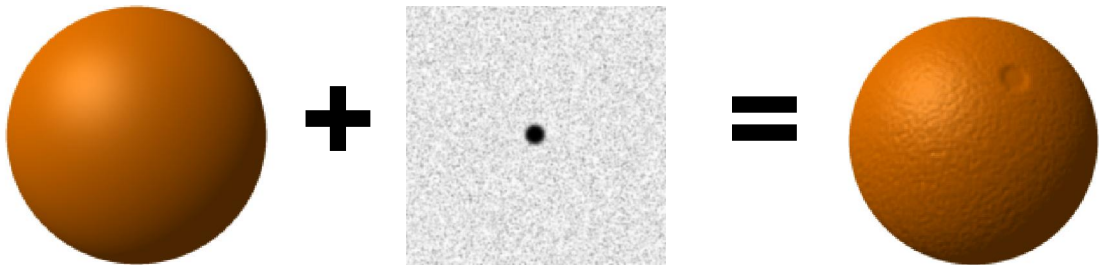






## Bump Mapping [1]: Basic Concept

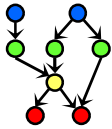
- Goal: Create Illusion of Textured Surface



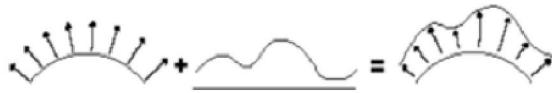
Bump Mapping © 2010 Wikipedia  
[http://en.wikipedia.org/wiki/Bump\\_mapping](http://en.wikipedia.org/wiki/Bump_mapping)

- Idea
  - \* Start with regular smooth object
  - \* Make height map (by hand and/or using program, *i.e.*, procedurally)
  - \* Use map to perturb surface normals
  - \* Plug new normals into illumination equation
- Will This Look Realistic? Why/Why Not?





## Bump Mapping [2]: Techniques



$$\mathbf{P}(u, v)$$

$$\mathbf{S}(u, v) = \frac{\partial \mathbf{P}(u, v)}{\partial u} \quad \mathbf{T}(u, v) = \frac{\partial \mathbf{P}(u, v)}{\partial v}$$

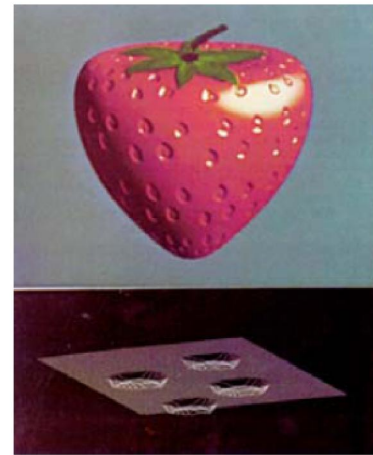
$$\mathbf{N}(u, v) = \mathbf{S} \times \mathbf{T}$$

### ■ Displacement

$$\mathbf{P}'(u, v) = \mathbf{P}(u, v) + h(u, v)\mathbf{N}(u, v)$$

### ■ Perturbed normal

$$\begin{aligned} \mathbf{N}'(u, v) &= \mathbf{P}'_u \times \mathbf{P}'_v \\ &= \mathbf{N} + h_u(\mathbf{T} \times \mathbf{N}) + h_v(\mathbf{S} \times \mathbf{N}) \end{aligned}$$

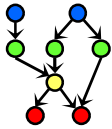


From Blinn 1976

Adapted from slides © 1995 – 2009 P. Hanrahan, Stanford University

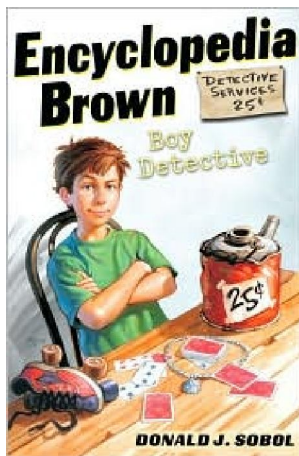
<http://bit.ly/hZfsjZ> (CS 348B)



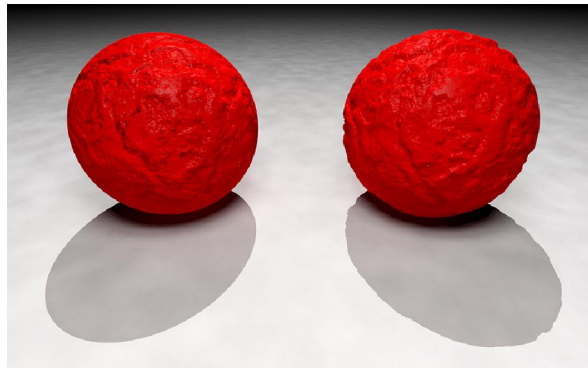


## Bump Mapping [3]: Advanced Methods & Research

- Bump Mapping Tutorial for OpenGL (Baker, 2003): <http://bit.ly/fun4a5>



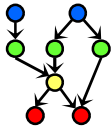
Hey, wait a minute!



... what's wrong with the one on the left?

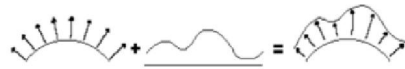
- Right Ball (Displacement Mapped) Casts *Rough* Shadow
- Left Ball (Bump Mapped) Casts *Smooth* Shadow – Why?
- Bump Mapping Only Perturbs Normals (Surface Only!)





## Displacement Mapping [1]: Basic Concept

- Remember What We Did to Perform Bump Mapping?



$$\mathbf{P}(u, v)$$

$$\mathbf{S}(u, v) = \frac{\partial \mathbf{P}(u, v)}{\partial u} \quad \mathbf{T}(u, v) = \frac{\partial \mathbf{P}(u, v)}{\partial v}$$

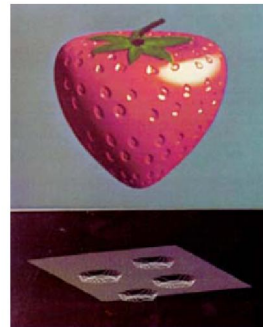
$$\mathbf{N}(u, v) = \mathbf{S} \times \mathbf{T}$$

### ■ Displacement

$$\mathbf{P}'(u, v) = \mathbf{P}(u, v) + h(u, v)\mathbf{N}(u, v)$$

### ■ Perturbed normal

$$\begin{aligned} \mathbf{N}'(u, v) &= \mathbf{P}'_u \times \mathbf{P}'_v \\ &= \mathbf{N} + h_u(\mathbf{T} \times \mathbf{N}) + h_v(\mathbf{S} \times \mathbf{N}) \end{aligned}$$



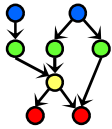
From Blinn 1976

- Q: Can We Make This *Permanent*? How?
- A: Sure! Let Perturbed Normals Define New Surface; Save Out Vertices

Adapted from slides © 1995 – 2009 P. Hanrahan, Stanford University

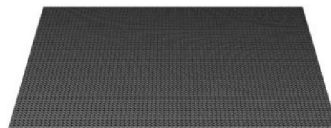
<http://bit.ly/hZfsjZ> (CS 348B)





## Displacement Mapping [2]: Techniques

- **Displacement Map: Similar to Bump Map – Contains Delta Values**



ORIGINAL MESH



DISPLACEMENT MAP



MESH WITH DISPLACEMENT

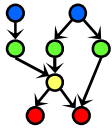


**Displacement Mapping:  
For Real!**

*Displacement Mapping* © 2005 Wikipedia  
[http://en.wikipedia.org/wiki/Displacement\\_mapping](http://en.wikipedia.org/wiki/Displacement_mapping)

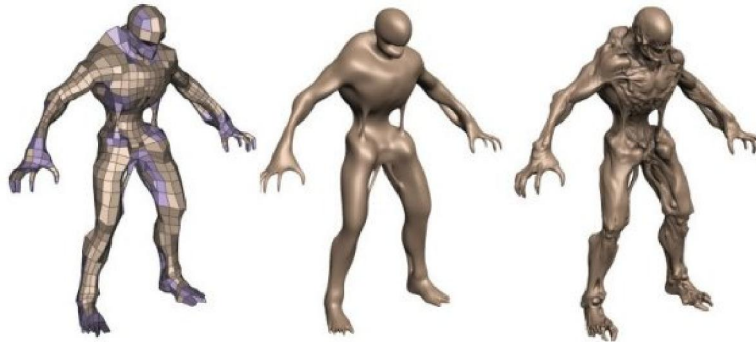
- **Displacement Mapping: Uses Open GL Shading Language (GLSL)**
- **Tutorial using GLSL (Guinot, 2006): <http://bit.ly/dWXNya>**





## Displacement Mapping [3]: Advanced Methods & Research

- **When To Consider Using Displacement Mapping**
  - ✦ Very “deep” texture effect: veins, ridges, etc.
  - ✦ Shadows expected

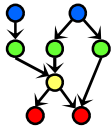


The “Imp” © Kenneth Scott, id Software 2008

The “Imp” © 2008 K. Scott, id Software  
Bjorn3D, <http://bit.ly/i78SiP>

**Like Many Mappings and Other Effects, Wanted In Hardware!**





## Acknowledgements: Texture Mapping Slides



**Andy van Dam**  
T. J. Watson University Professor of  
Technology and Education &  
Professor of Computer Science  
Brown University  
<http://www.cs.brown.edu/~avd/>



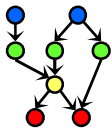
Texture Mapping

Beautification of Surfaces

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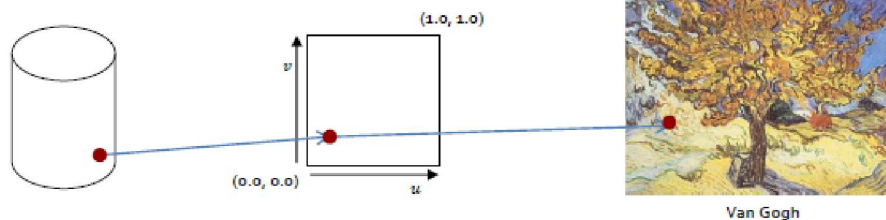






## Texture Mapping Technique [1]

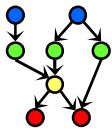
- ▶ Texture mapping is the process of mapping a geometric point in space to a value (color, normal, other...) in a texture
- ▶ Our goal is to map any arbitrary geometry to a texture of any dimension
- ▶ This is done in two steps:
  - ▶ Map a point on the geometry to a point on the unit square
  - ▶ Map the unit square point to point on the texture



- ▶ Second mapping is much easier, we'll present it first.

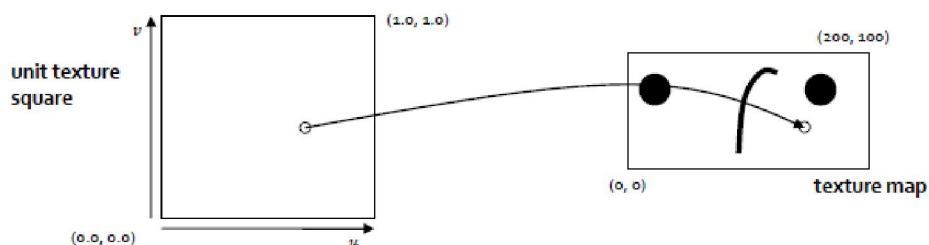
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## Texture Mapping Technique [2]

- ▶ Mapping a point in the unit  $u, v$  square to a texture of arbitrary dimension:
  - ▶ In general, any point  $(u, v)$  on the unit square, the corresponding point on the texture of length  $l$  pixels and height  $h$  pixels is  $(u * l, v * h)$ .

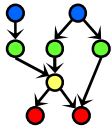


- ▶ Above:  $(0.0, 0.0) \rightarrow (0, 0)$ ;  $(1.0, 1.0) \rightarrow (200, 100)$ ;  $(.7, .45) \rightarrow (140, 45)$
- ▶ Once we have coordinates for the texture, we just need to look up the color of the texture at these coordinates
- ▶ Coordinates not always a discrete point on texture as they come from continuous space. May need to average neighboring texture pixels (i.e. filter)

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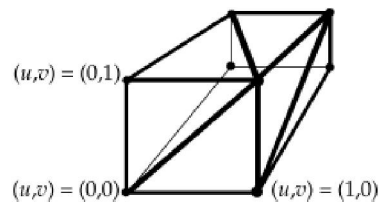
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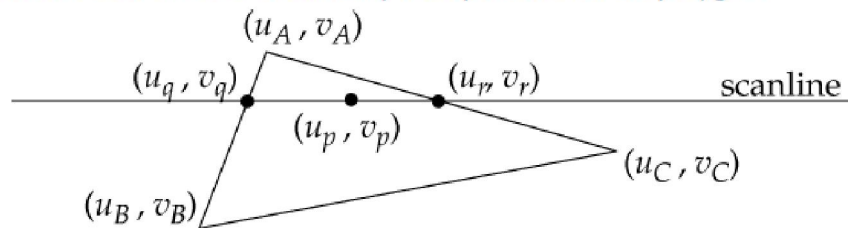


## Texture Mapping Technique [3]

- ▶ Texture mapping polygons
  - ▶  $(u, v)$  texture coordinates are pre-calculated and specified per vertex
  - ▶ Vertices may have different texture coordinates for different faces

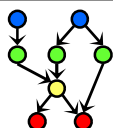


- ▶ Texture coordinates are linearly interpolated across polygon



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## Interpolation Trick: Barycentric Coordinates

- ▶ Consider interpolating between two values along a line
  - ▶ Given two colors  $C_a$  and  $C_b$ , you can compute any value along the "line" between the two colors by evaluating:

$$C(t) = (1 - t)C_a + tC_b \quad 0 \leq t \leq 1$$

- ▶ This equation can be written as:

$$C(s, t) = sC_a + tC_b \quad s + t = 1 \quad s, t \geq 0$$

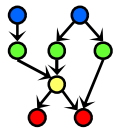
- ▶  $s$  and  $t$  are the Barycentric Coordinates of the line segment between  $C_a$  and  $C_b$
- ▶ The EQ of the line is a convex linear combination of its endpoints. We've seen this before (splines, color theory)
- ▶ Barycentric coordinates can be generalized to triangles

$$C(s, t, u) = sC_a + tC_b + uC_c \quad s + t + u = 1 \quad s, t, u \geq 0$$

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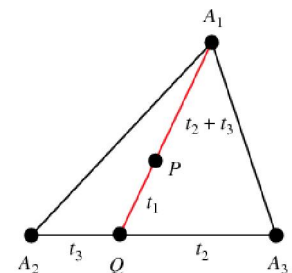
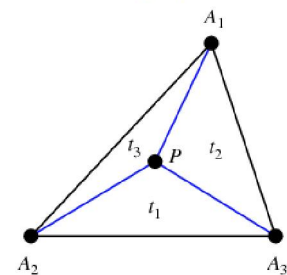
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## Applying Barycentric Coordinates

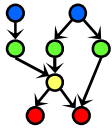
- ▶ When you intersect a ray with a polyhedral object (not needed for our intersect/ray projects):
  - ▶ return the vertex data of the triangle intersected
  - ▶ return the Barycentric coordinates  $(t_1, t_2, t_3)$  of the intersection point
  - ▶ These coordinates can be used to interpolate between vertex colors, normals, texture coordinates, or other data
  - ▶ What weights do we hang on each vertex such that the triangle would be perfectly balanced on a pin at point  $P$
  - ▶ Alternatively, think of a mobile suspended from  $P$  with 2 arms  $A_1Q$  and  $A_2A_3$ .
- ▶ Compute  $Q$  as intersection of line through  $A_1$  and  $P$  and line through  $A_2$  and  $A_3$
- ▶  $t_3' = |Q - A_2|$
- ▶  $t_2' = |Q - A_3|$
- ▶  $t_1' = |P - Q|$
- ▶  $(t_1, t_2, t_3) = (t_1', t_2', t_3') / (t_1' + t_2' + t_3')$
- ▶ Another way of thinking about this is by triangle area. The weight at  $A_1$  should be proportional to the area of the triangle  $P, A_2, A_3$ , and so on...



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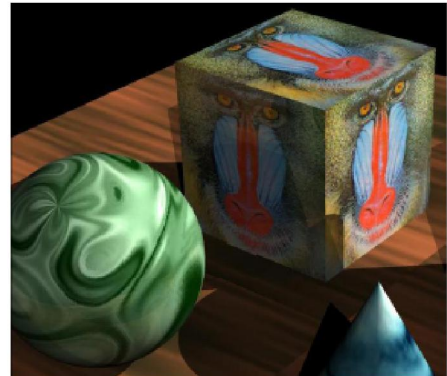
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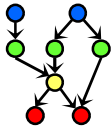
## Texture Mapping Technique [4]: Map Point to Object on $(u, v)$ Square

- ▶ Texture mapping in "Ray": mapping solids
  - ▶ Using ray tracing, we obtain an intersection point  $(x, y, z)$  in object space
  - ▶ We need to map this point to a point on the  $(u, v)$  unit square, so we can map that to a texture value
  - ▶ Three easy cases: planes, cylinders, and spheres
- ▶ Easiest to compute the mapping from  $(x, y, z)$  coordinates in **object space** to  $(u, v)$
- ▶ Can cause unwanted texture scaling
- ▶ Texture filtering is an option in most graphics libraries
- ▶ OpenGL allows you to choose filtering method. (GL\_NEAREST, GL\_LINEAR, etc...)



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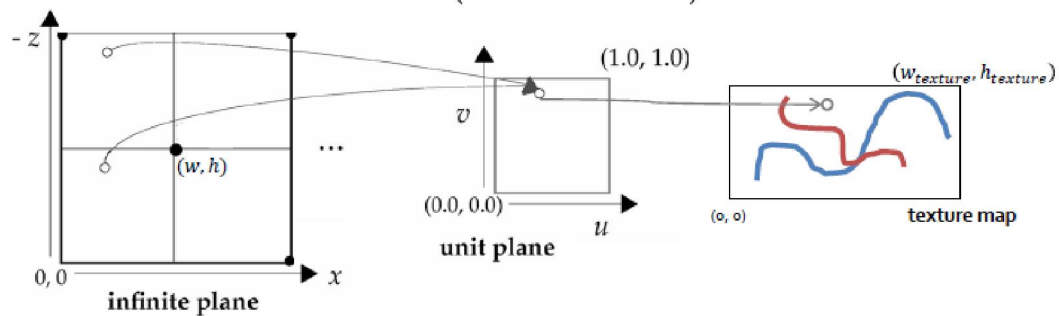




## Texture Mapping Technique [5]

- ▶ Texture mapping large quads:
  - ▶ How to map a point on a very large quad to a point on the unit square?
  - ▶ Tiling: texture is repeated over and over across infinite plane
  - ▶ Given coordinates  $(x, y)$  of a point on an arbitrarily large quad that we want to tile with quads of size  $(w, h)$ , the  $(u, v)$  coordinates on the unit square representing a texture with arbitrary dimensions are:

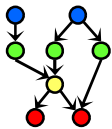
$$(u, v) = \left( \frac{(x \% w)}{w}, \frac{(y \% h)}{h} \right)$$



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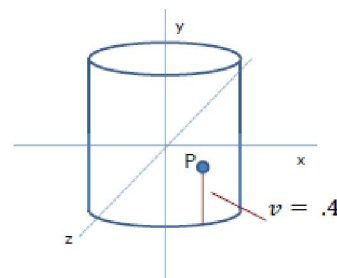
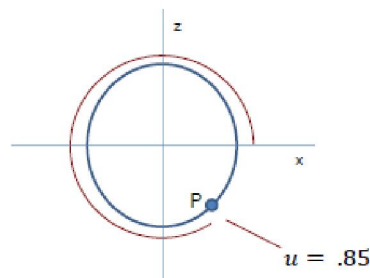
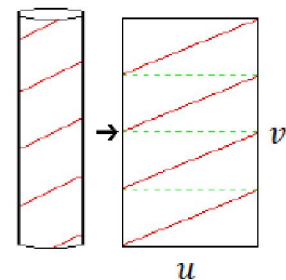


## Texture Mapping Technique [6]

### ► How to texture map cylinders and cones:

#### ► Given a point P on the surface:

- If it's on one of the caps, map as though the cap is a plane
- If it's on the curved surface:
  - Use the position of the point around the perimeter to determine  $u$
  - Use the height of the point to determine  $v$

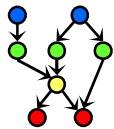


#### ► Mapping $v$ is trivial, $[-.5, .5]$ gets mapped to $[0.0, 1.0]$ just by adding $.5$

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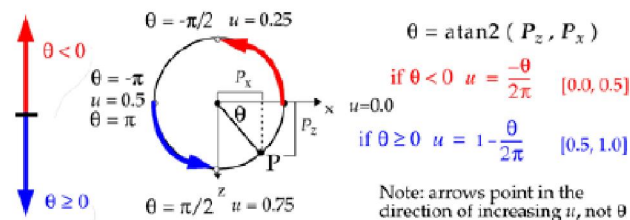
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## Texture Mapping Technique [7]

- ▶ Computing the  $u$  coordinate for cones and cylinders:
  - ▶ We need to map all the points on the perimeter of the object to  $[0, 1]$ .
  - ▶ The easiest way is to say  $u = \frac{\theta}{2\pi}$ , but computing  $\theta$  can be tricky

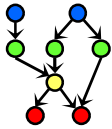


- ▶ Standard atan function computes a result for  $\theta$  but its always between 0 and  $\pi$  and it maps two positions on the perimeter to the same  $\theta$  value.
  - ▶ Example:  $\text{atan}(1, 1) = \text{atan}(-1, -1) = \frac{\pi}{2}$
- ▶  $\text{atan2}(x, y)$  yields values between  $-\pi$  and  $\pi$ , but isn't continuous. See above diagram.

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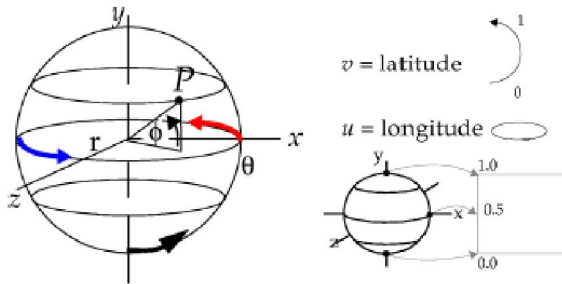




## Texture Mapping Technique [8]

### ► Texture mapping spheres:

- Find  $(u, v)$  coordinates for  $P$
- We compute  $u$  the same we do for cylinders and cones
- If  $v = 0$  or  $v = 1$ , there is a singularity. Set  $u$  to some predefined value. (.5 is good)
- $v$  is a function of the latitude of  $P$

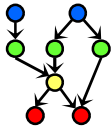


$$\phi = \sin^{-1} \frac{P_y}{r} \quad -\frac{\pi}{2} \leq \phi < \frac{\pi}{2} \quad r = \text{radius}$$

$$v = \frac{\phi}{\pi} + .5$$

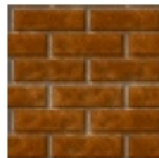
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## Texture Mapping Style [1]: Tiling

- ▶ We want to create a brick wall with a brick pattern texture
  - ▶ A brick pattern is very repetitive, we can use a small texture and “tile” it across the wall

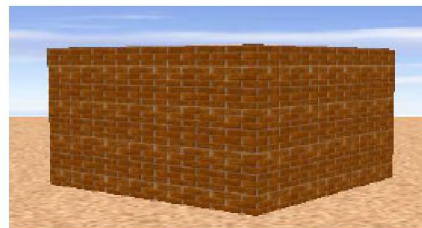


Texture



Without Tiling

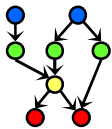
- ▶ Tiling allows you to scale repetitive textures to make texture elements just the right size.



With Tiling

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## Texture Mapping Style [2]: Stretching

- ▶ With non-repetitive textures, we have less flexibility
  - ▶ Have to fill an arbitrarily large object with a texture of finite size
  - ▶ Can't tile, have to stretch
- ▶ Example, creating a sky backdrop:



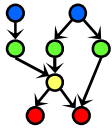
Texture



Applied with stretching

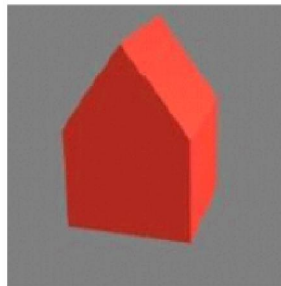
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## Texture Mapping Complex Geometry [1]

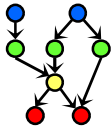
- ▶ Sometimes, reducing objects to primitives for texture mapping doesn't achieve the right result.
- ▶ Consider a simple house shape as an example
- ▶ If we texture map it by our old methods, we get discontinuities at some edges.



- ▶ Solution: Pretend object is a sphere and texture map using the sphere  $(u, v)$  map

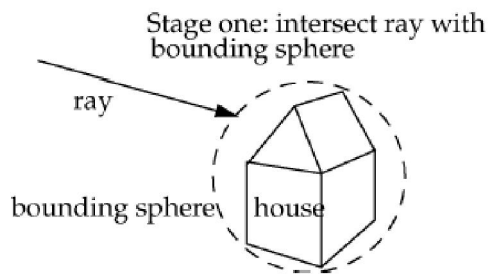
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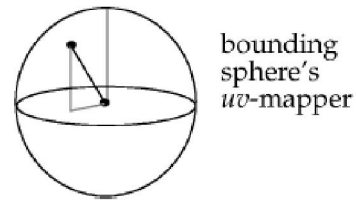


## Texture Mapping Complex Geometry [2]

- ▶ Intuitive approach: Place a bounding sphere around the complex object
  - ▶ Find ray's object space intersection with bounding sphere
  - ▶ Convert to  $(u, v)$  coordinates



Stage two: calculate intersection point's  $uv$ -coords

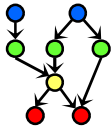


- ▶ We actually don't need a bounding sphere!
  - ▶ Once we have the intersection point with the object, we just treat it as though it were on the sphere. Same results, but be careful with radii.

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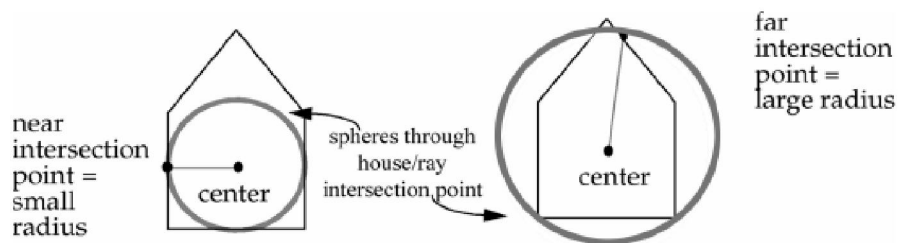






## Texture Mapping Complex Geometry [3]

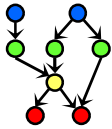
- ▶ When we treat the object intersection point as a point on a sphere, our “sphere” won’t always have the same radius



- ▶ What radius to use?
  - ▶ Compute the radius as the distance from the center of the complex object to the intersection point. Use that as the radius for the  $(u, v)$  mapping.

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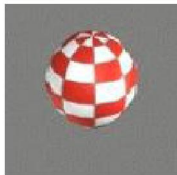


## Texture Mapping Complex Geometry [4]

- ▶ Results of spherical ( $u, v$ ) mapping:
- ▶ You can use cylindrical or planar mappings for complex objects as well
- ▶ Each has drawbacks
  - ▶ Spherical: warping at the "poles" of the object
  - ▶ Cylindrical: discontinuities at the caps
  - ▶ Planar: one dimension must be ignored



sphere  
mapped with  
spherical  
projection

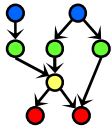


sphere mapped  
with planar  
projection

- ▶ For best overall results, mapping techniques can be swapped

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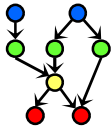
## OpenGL Texturing [1]: Steps

- Create and specify a texture object
  - Create a texture object
  - Specify the texture image
  - Specify how texture has to be applied for each pixel
- Enable texture mapping
- Draw the textured polygons
  - Identify the active texture
  - Specify texture coordinates with vertices

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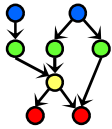
## OpenGL Texturing [2]: Specify 2-D Texture Object

- **`glTexImage2D`**(GLenum *target*, GLint *level*, GLint *internalformat*, GLsizei *width*, GLsizei *height*, GLint *border*, GLenum *format*, GLenum *type*, const GLVoid \**texels*);
  - Eg: **`glTexImage2D`**(GL\_TEXTURE\_2D, 0, GL\_RGBA, 128, 128, 0, GL\_RGBA, GL\_UNSIGNED\_BYTE, *image*);
  - *format* and *type* used to specify the way the texels are stored
  - *internalFormat* specifies how OpenGL should store the data internally
  - *width* and *height* have to be powers of 2; you can use **`gluScaleImage`**( ) to scale

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## OpenGL Texturing [3]: Specify How Texture Is Applied

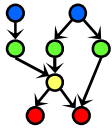
- **`glTexParameter{if}(GLenum target, GLenum pname, TYPE param)`**
- **`target`** can be: `GL_TEXTURE_1D`, `GL_TEXTURE_2D`, ...

<i><b>pname</b></i>	<i><b>param</b></i>
<code>GL_TEXTURE_WRAP_S</code>	<code>GL_CLAMP</code> , <code>GL_REPEAT</code>
<code>GL_TEXTURE_WRAP_T</code>	<code>GL_CLAMP</code> , <code>GL_REPEAT</code>
<code>GL_TEXTURE_MAG_FILTER</code>	<code>GL_NEAREST</code> , <code>GL_LINEAR</code>
<code>GL_TEXTURE_MIN_FILTER</code>	<code>GL_NEAREST</code> , <code>GL_LINEAR</code>

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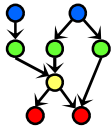
## OpenGL Texturing [4]: Enable Texture and Draw

- ***glEnable***(GL\_TEXTURE\_2D)
  - Enable 2D texturing
- ***glTexCoord2f***(GL\_FLOAT *u*, GL\_FLOAT *v*)
  - Specify texture coordinates per vertex (just as normals, color, etc).

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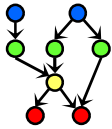
## OpenGL Texturing [5]: Create Texture Object

- ***glGenTextures***(GLsizei *n*, GLuint\* *textureIDs*);
  - Returns *n* currently unused texture ID in *textureIDs*
  - Each texture ID is an integer greater than 0
- ***glBindTexture***(GLenum *target*, GLuint *textureID*);
  - *target* is GL\_TEXTURE\_1D, GL\_TEXTURE\_2D, or GL\_TEXTURE\_3D
  - if *textureID* is being used for the first time a new texture object is created and assigned the ID = *textureID*
  - if *textureID* has been used before, the texture object with ID = *textureID* becomes active

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## OpenGL Texturing [6]: Putting It All Together

In initialization:

```
glGenTextures(...);  
glBindTexture( ... );  
glTexParameterf(...); glTexParameterf(...); ...  
glTexImage2D(...);  
glEnable(GL_TEXTURE_2D);
```

In display:

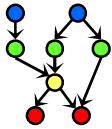
```
glBindTexture( ... ); // Activate the texture defined in  
initialization  
glBegin(GL_TRIANGLES);  
glTexCoord2f(...); glVertex3f(...);  
glTexCoord2f(...); glVertex3f(...);  
glTexCoord2f(...); glVertex3f(...);  
glEnd( );
```

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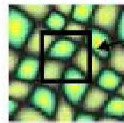
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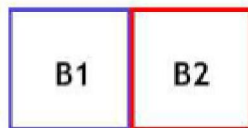


## Preview: Texturing with Blocks

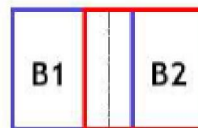


block

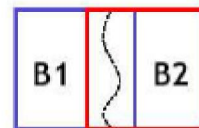
Input texture



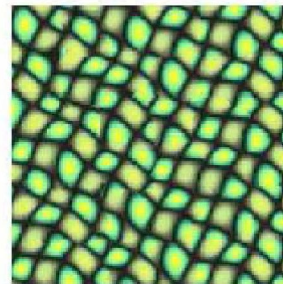
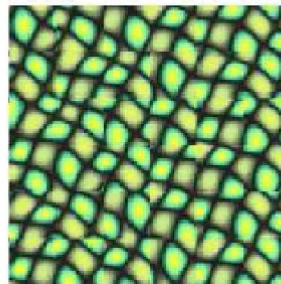
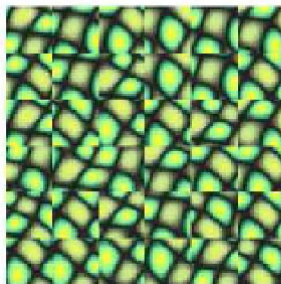
Random placement  
of blocks



Neighboring blocks  
constrained by overlap



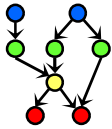
Minimal error  
boundary cut



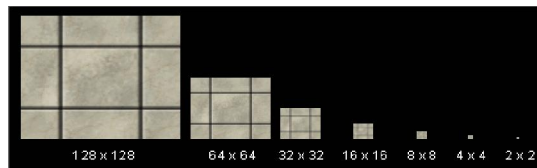
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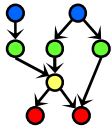
## Preview: Mipmapping



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## Summary

- **Last Time: Texture Mapping Explained**

- \* Definitions and design principles
- \* Enclosing volumes: cylinder, sphere, box
- \* Mapping methods
  - reflected ray
  - object normal
  - object center
  - intermediate surface normal

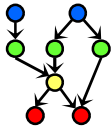


*The Lord of the Rings:  
The Fellowship of the Ring*  
© 2001 New Line Cinema

- **Today: Mappings, OpenGL Texturing**

- \* Idea: define “texture” to simulate surface detail
- \* Shadow, reflection/environment, transparency, bump, displacement
- \* Other mappings: gloss, volumetric fog, skins, rainbows, water
- \* OpenGL texture mapping how-to





## Terminology

- **Texture Mapping - Adding Detail, Raster Image, Color, etc. to CG Model**
  - \* Planar projection: apply flat texture to flat surface(s)
  - \* Enclosing volumes: cylinder, sphere, box
  - \* Mapping methods
    - reflected ray – bounce ray off object  $O$
    - object normal – ray from face normal of object (polygon mesh)
    - object center – ray from center of object
    - intermediate surface normal – ray from inside of enclosing  $S$
- **Mappings: Apply Image or Simulated Surface Detail to Object**
  - \* Shadow: cast planar projective shadows or calculate volume
  - \* Reflection/environment: take picture of scene from “inside” object
  - \* Transparency: take picture of scene “behind” object; refract
  - \* Bump: perturb color based on height map
  - \* Displacement: perturb face normals, recalculate lighting

