



## Lecture 23 of 41

### More Rotations; Visualization, Simulation Videos 4: Virtual & Augmented Reality, Viz-Sim

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KSOL course pages: <http://bit.ly/hGvXIH> / <http://bit.ly/eVizrE>  
Public mirror web site: <http://www.kddresearch.org/Courses/CIS636>  
Instructor home page: <http://www.cis.ksu.edu/~bhsu>

#### Readings:

Today: Chapter 10, 13, §17.3 – 17.5, Eberly 2<sup>e</sup> – see <http://bit.ly/leUq45>  
Next class: §2.4.3, 8.1, Eberly 2<sup>e</sup>, [GL handout](#)  
Wikipedia, Visualization: <http://bit.ly/gVxRFp>  
Wikipedia on quaternions: <http://bit.ly/f1GvTS>, <http://bit.ly/eBnCY4>  
Reference: Ogre Wiki quaternion primer – <http://bit.ly/hv6zv0>



## Lecture Outline

- Reading for Last Class: §17.1 – 17.2, Eberly 2<sup>e</sup>
- Reading for Today: Chapter 10, 13, §17.3 – 17.5, Eberly 2<sup>e</sup>
- Reading for Next Class: §2.4.3, 8.1, Eberly 2<sup>e</sup>, [GL handout](#)
- Last Time: Rotations in Animation
  - \* Flight dynamics: roll, pitch, yaw
  - \* Matrix, angles (fixed, Euler, axis), quaternions, exponential maps
- Quaternions Concluded
  - \* How quaternions work – properties (review)
    - Equivalent rotation matrix (RM)
    - Quaternion arithmetic
    - Composition of rotations by quaternion multiplication
  - \* Advantage: easy incremental rotation; camera, character animation
- Today: Intro to Visualization, Modeling & Simulation
  - \* Virtual reality (VR), virtual environments (VE)
  - \* Augmented reality (AR)



## Where We Are

21	Lab 4a: Animation Basics	Flash animation handout
22	Animation 2: Rotations, Dynamics, Kinematics	Chapter 17, esp. §17.1 – 17.2
23	Demos 4: Modeling & Simulation, Rotations	Chapter 10, 13, §17.3 – 17.5
24	Collisions 1: axes, OBBs, Lab 4b	§2.4.3, 8.1, <a href="#">GL handout</a>
25	Spatial Sorting, Binary Space Partitioning	Chapter 6, esp. §6.1
26	Demos 8: More CGA, Picking, HW Exam	Chapter 7, § 8.4
27	Lab 5a: Interaction Handling	§ 8.3 – 8.4, 4.2, 5.0, 5.6, 9.1
28	Collisions 2: Dynamic, Particle Systems	§ 9.1, particle system handout
29	Exam 2 review; Hour Exam 2 (evening)	Chapters 5 – 6, 7 <sup>e</sup> – 8, 12, 17
29	Lab 5b: Particle Systems	Particle system handout
30	Animation 3: Control & IK	§ 9.3, CGA handout
31	Ray Tracing 1: Intersections, ray trees	Chapter 14
32	Lab 6a: Ray Tracing Basics with POV-Ray	RT handout
33	Ray Tracing 2: advanced topic survey	Chapter 15, RT handout
34	Visualization 1: Data (Quantities & Evidence)	Tufte handout (1)
35	Lab 6b: More Ray Tracing	RT handout
36	Visualization 2: Objects	Tufte handout (2 & 4)
37	Color Basics, Term Project Prep	Color handout
38	Lab 7: Fractals & Terrain Generation	Fractals/Terrain handout
39	Visualization 3: Processes; Final Review 1	Tufte handout (3)
40	Project presentations 1; Final Review 2	–
41	Project presentations 2	–
	Final Exam	Ch. 1 – 8, 10 – 16, 17, 20

Lightly-shaded entries denote the due date of a written problem set; heavily-shaded entries, that of a machine problem (programming assignment); blue-shaded entries, that of a paper review, and the green-shaded entry, that of the term project.  
Green, blue and red letters denote exam review, exam, and exam solution review dates.



## Acknowledgements: CGA Rotations, Dynamics & Kinematics



**Rick Parent**  
Professor  
Department of Computer Science and Engineering  
Ohio State University  
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**David C. Brogan**  
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<http://www.sig.com>



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## Review [1]: Representing 3 Rotational DOFs

### 3x3 Matrix (9 DOFs)

- Rows of matrix define orthogonal axes

### Euler Angles (3 DOFs)

- Rot x + Rot y + Rot z

### Axis-angle (4 DOFs)

- Axis of rotation + Rotation amount

### Quaternion (4 DOFs)

- 4 dimensional complex numbers



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## Review [2]: Method 1 Rotation Matrices – Roll, Pitch, & Yaw

Rotation about x axis  
(Roll)

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(\alpha) & -\sin(\alpha) & 0 \\ 0 & \sin(\alpha) & \cos(\alpha) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Rotation about y axis  
(Pitch)

$$\begin{bmatrix} \cos(\beta) & 0 & \sin(\beta) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(\beta) & 0 & \cos(\beta) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



© Wikipedia,  
fr Dynamics  
[bit.ly/vaGQX](http://bit.ly/vaGQX)


Rotation about z axis  
(Yaw)

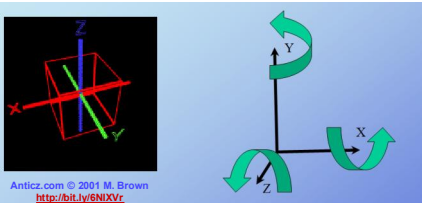
$$\begin{bmatrix} \cos(\gamma) & -\sin(\gamma) & 0 & 0 \\ \sin(\gamma) & \cos(\gamma) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



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CSE 682 (Computer Animation), <http://bit.ly/teUESy>  
CSE 683/684 (Computer Animation Algorithms & Techniques), <http://bit.ly/f8Myky>



7  **Review [3]: Method 2  
Fixed Angles & Gimbal Lock**




Anticiz.com © 2001 M. Brown  
<http://bit.ly/6NIXVr>

$$(\alpha \quad \beta \quad \gamma) \rightarrow P' = R_z(\gamma)R_y(\beta)R_x(\alpha)P$$

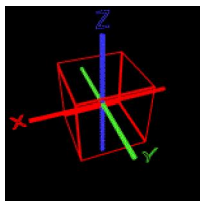

Fixed order: e.g., x, y, z; also could be x, y, x  
Global axes

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8  **Gimbal Lock Illustrated [1]**


- **Gimbal Lock:** Loss of DOF when 2 of 3 Gimbals Driven until Parallel
- **Animated Examples**
  - \* e.g., x & z (left), y & z (right)
  - \* **Caution:** Seefeld (right) refers to these as “x” (red) & z (blue)
  - \* y (Pitch) = “x”, x (Roll) = “y”, z (Yaw) = “z” (“zed”)

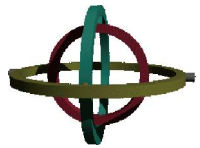
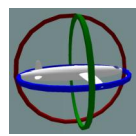
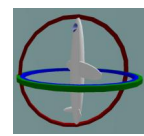
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<http://bit.ly/e1nuo2>

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9  **Gimbal Lock Illustrated [2]**


- Gimbals: 2 of 3 Driven into Parallel Configuration
- Happens With Euler Angles Too: <http://bit.ly/g32DQ5> (Wikipedia)
- **Solution Approaches**
  - \* Extra gimbal
  - \* **Quaternions:**  $(\cos(\theta/2), x_0 \cdot \sin(\theta/2), y_0 \cdot \sin(\theta/2), z_0 \cdot \sin(\theta/2))$ .  $\vec{N} = (x_0, y_0, z_0)$

Gimbal Lock figure © 2006 Wikipedia  
(Rendered using POV-Ray)  
<http://bit.ly/hR8vY2>

Left: not locked  
Right: x & z rotations locked (roll & pitch, no yaw)  
Gimbal Lock figures © 2009 Wikipedia  
<http://bit.ly/h8LNS>

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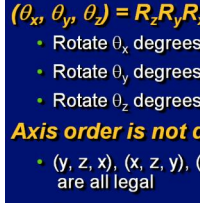
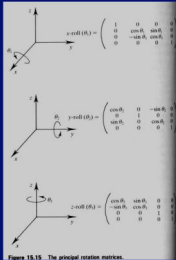
10  **Review [4]: Method 3  
Euler Angles & Order Independence**

$(\theta_x, \theta_y, \theta_z) = R_z R_y R_x$

- Rotate  $\theta_x$  degrees about x-axis
- Rotate  $\theta_y$  degrees about y-axis
- Rotate  $\theta_z$  degrees about z-axis

**Axis order is not defined**


- (y, z, x), (x, z, y), (z, y, x) ... are all legal
- Pick one

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11  **Review [5]:  
Euler Angle Sequences**


- This means that we can represent an orientation with 3 numbers
- A sequence of rotations around principal axes is called an *Euler Angle Sequence*
- Assuming we limit ourselves to 3 rotations without successive rotations about the same axis, we could use any of the following 12 sequences:

XYZ	XZY	YXZ	YZX
YXZ	YZX	ZXY	ZYX
ZXY	ZYX	XZY	YZX
YZX	XZY	YXZ	YZX

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12  **Using Euler Angles [1]:  
Representing Orientations**

- This gives us  $3! + C(3, 2) * 2 = 6 + 3 * 2 = 12$  redundant ways to store an orientation using Euler angles
- Different industries use different conventions for handling Euler angles (or no conventions)

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15  **Using Euler Angles [2]:  
Conversion: Euler Angle to RM**


■ To build a matrix from a set of Euler angles, we just multiply a sequence of rotation matrices together:

$$\mathbf{R}_x \cdot \mathbf{R}_y \cdot \mathbf{R}_z = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_x & s_x \\ 0 & -s_x & c_x \end{bmatrix} \cdot \begin{bmatrix} c_y & 0 & -s_y \\ 0 & 1 & 0 \\ s_y & 0 & c_y \end{bmatrix} \cdot \begin{bmatrix} c_z & s_z & 0 \\ -s_z & c_z & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} c_y c_z & c_y s_z & -s_y \\ s_x s_y c_z - c_x s_z & s_x s_y s_z + c_x s_z & s_x c_y \\ c_x s_y c_z + s_x s_z & c_x s_y s_z - s_x s_z & c_x c_y \end{bmatrix}$$

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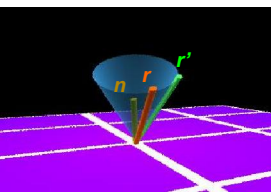
14  **Review [6]: Method 4  
Axis-Angle: Specification**

Given

- $\mathbf{r}$  – vector in space to rotate
- $\mathbf{n}$  – unit-length axis in space about which to rotate
- $\alpha$  – amount about  $\mathbf{n}$  to rotate


Solve

$\mathbf{r}'$  – rotated vector



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15  **Review [7]: Method 5  
Quaternions to RM, Axis-Angle**

$$\text{Rot}_{[s \ x \ y \ z]} = \begin{bmatrix} 1-2y^2-2z^2 & 2xy-2sz & 2xz-2sy \\ 2xy-2sz & 1-2x^2-2z^2 & 2yz-2sx \\ 2xz-2sy & 2yz-2sx & 1-2x^2-2y^2 \end{bmatrix}$$

Axis-Angle  $\begin{cases} \theta = 2 \cos^{-1}(s) \\ (x, y, z) = \mathbf{v} / \|\mathbf{v}\| \end{cases}$

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16  **Quaternions [1]:  
Basic Idea**

**Remember complex numbers:  $a + ib$**

- Where  $i^2 = -1$

**Invented by Sir William Hamilton (1843)**


- Remember Hamiltonian path from Discrete Math?

**Quaternion:**

- $Q = a + bi + cj + dk$ 
  - Where  $i^2 = j^2 = k^2 = -1$  and  $ij = k$  and  $ji = -k$
- Represented as:  $q = (s, \mathbf{v}) = s + v_x i + v_y j + v_z k$

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17  **Quaternions [2]:  
Definition**

**A quaternion is a 4-D unit vector  $q = [x \ y \ z \ w]$**

- It lies on the unit hypersphere  $x^2 + y^2 + z^2 + w^2 = 1$


**For rotation about (unit) axis  $\mathbf{v}$  by angle  $\theta$**

- vector part =  $(\sin \theta/2) \mathbf{v} = [x \ y \ z]$
- scalar part =  $(\cos \theta/2) = w$
- $(\sin(\theta/2) n_x, \sin(\theta/2) n_y, \sin(\theta/2) n_z, \cos(\theta/2))$

**Only a unit quaternion encodes a rotation - normalize**

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18  **Quaternions [3]:  
Equivalent RM & Composition**

**Rotation matrix corresponding to a quaternion:**


- $[x \ y \ z \ w] = \begin{bmatrix} 1-2y^2-2z^2 & 2xy+2wz & 2xz-2wy \\ 2xy-2wz & 1-2x^2-2z^2 & 2yz+2wx \\ 2xz+2wy & 2yz-2wx & 1-2x^2-2y^2 \end{bmatrix}$

**Quaternion Multiplication**

- $q_1 * q_2 = [v_1, w_1] * [v_2, w_2] = [(w_1 v_2 + w_2 v_1 + (v_1 \times v_2)), w_1 w_2 - v_1 \cdot v_2]$
- quaternion \* quaternion = quaternion
- this satisfies requirements for mathematical group
- Rotating object twice according to two different quaternions is equivalent to one rotation according to product of two quaternions

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19  **Quaternions [4]: Examples**

**X-roll (roll) of  $\pi$**

- $(\cos(\pi/2), \sin(\pi/2)(1, 0, 0)) = (0, (1, 0, 0))$

**Y-roll (pitch) of  $\pi$**

- $(0, (0, 1, 0))$

**Z-roll (yaw) of  $\pi$**


- $(0, (0, 0, 1))$

**$R_y(\pi)$  followed by  $R_z(\pi)$**

- $(0, (0, 1, 0)) \text{ times } (0, (0, 0, 1)) = (0, (0, 1, 0)) \times (0, (0, 0, 1)) = (0, (1, 0, 0))$

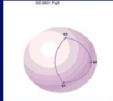
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20  **Quaternions [5]: Interpolation**

**Biggest advantage of quaternions**


- Interpolation
- Cannot linearly interpolate between two quaternions because it would speed up in middle
- Instead, Spherical Linear Interpolation, `slerp()`
- Used by modern video games for third-person perspective
- Why?



Hint: see <http://youtu.be/-jBKKV2V8eU>

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21  **Quaternions [6]: Spherical Linear Interpolation (SLERP)**

**Quaternion is a point on the 4-D unit sphere**

- interpolating rotations requires a unit quaternion at each step
  - another point on the 4-D unit sphere
- move with constant angular velocity along the great circle between two points


**Any rotation is defined by 2 quaternions, so pick the shortest SLERP**

**To interpolate more than two points, solve a non-linear variational constrained optimization**

- Ken Shoemake in SIGGRAPH '85 ([www.acm.org/dl](http://www.acm.org/dl))

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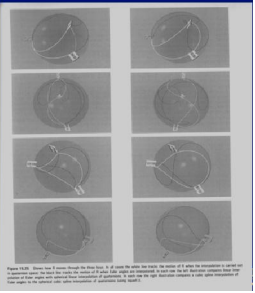
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22  **Quaternions [7]: Comparison with Euler Interpolation**

**Quaternion (white) vs. Euler (black) interpolation**


**Left images are linear interpolation**

**Right images are cubic interpolation**



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23  **Quaternions [8]: Code**

- Gamasutra (1998): <http://bit.ly/dQy8Cp>
- Nate Robins's Implementation: <http://bit.ly/fcGufq>
  - File `gltb.c`
  - `gltbMatrix`
  - `gltbMotion`

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24  **Spherical Interpolation [1]: Spheres**

- Think of a person standing on the surface of a big sphere (like a planet)
- From the person's point of view, they can move in along two orthogonal axes (front/back) and (left/right)
- There is no perception of any fixed poles or longitude/latitude, because no matter which direction they face, they always have two orthogonal ways to go
- From their point of view, they might as well be moving on a infinite 2D plane, however if they go too far in one direction, they will come back to where they started!

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## Spherical Interpolation [2]: Hyperspheres

- Now extend concept to moving in *hypersphere* of unit quaternions
- Now have three orthogonal directions to go
- No matter how oriented in this space, can always go some combination of forward/backward, left/right and up/down
- Go too far in any direction: back to start point
- Location on unit hypersphere: orientation
- Moving in arbitrary direction corresponds to rotating around some arbitrary axis

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## Review [8]: Dynamics & Kinematics

- Dynamics: Study of Motion & Changes in Motion**
  - Forward: model forces over time to find state, e.g.,
    - Given: initial position  $p_0$ , velocity  $v_0$ , gravitational constants
    - Calculate: position  $p_t$  at time  $t$
  - Inverse: given state and constraints, calculate forces, e.g.,
    - Given: *desired* position  $p_t$  at time  $t$ , gravitational constants
    - Calculate: position  $p_0$ , velocity  $v_0$  needed
  - Wikipedia: <http://bit.ly/hH43dX> (see also: "Analytical dynamics")
  - For non-particle objects: rigid-body dynamics (<http://bit.ly/dLveig>)
- Kinematics: Study of Motion without Regard to Causative Forces**
  - Modeling systems – e.g., articulated figure
  - Forward: from angles to position (<http://bit.ly/eh2d1c>)
  - Inverse: finding angles given desired position (<http://bit.ly/hsyTb0>)
  - Wikipedia: <http://bit.ly/hr8r2u>

Forward Kinematics © 2009 Wikipedia

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## Visualization [1]: Animating Simulations

Deepwater Horizon Oil Spill (20 Apr 2010)  
<http://bit.ly/9Qhax4>  
120-day images © 2010 NOAA, <http://t1.usa.gov/c2zuQ>

120-day simulation using 06 Apr 1996 weather conditions

120-day simulation using 17 Apr 1997 weather conditions

120-day simulation using 15 Apr 1993 weather conditions

132-day simulation using 2010 conditions  
© 2010 National Center for Supercomputing Applications (NCSA)  
[http://youtu.be/E-1G\\_476nA](http://youtu.be/E-1G_476nA)

Visualization Of An F3 Tornado Within A Supercell Thunderstorm Sim  
1,524 videos © YouTube

Wilhelmson et al. (2004)  
<http://youtu.be/EqumU0Ns1YI>  
<http://avi.ncsa.uiowa.edu>  
<http://bit.ly/sA8PXN>

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## Visualization [2]: Virtual Reality (VR)

- Virtual Reality: Computer-Simulated Environments**
- Physical Presence: Real & Imaginary**
- Hardware: User Interface**
  - Head-mounted display (HMD), gloves – see PopOptics goggles (left)
  - VR glasses, wand, etc. – see NCSA CAVE (right)

Virtual Reality, Wikipedia: <http://bit.ly/3dX8E>  
Image © 2007 National Air & Space Museum

CAVE (Cave Automatic Virtual Environment)  
Image © 2009 D. Pape  
HowStuffWorks article: <http://bit.ly/LyfeQnXk>  
© 2009 J. Strickland  
Wikipedia: <http://bit.ly/3dX8E>

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## Visualization [3]: Virtual Environments (VE)

- Virtual Environment: Part of Virtual Reality Experience**
- Other Parts**
  - Virtual artifacts (VA): simulated objects – <http://bit.ly/hskSyX>
  - Intelligent agents, artificial & real – <http://bit.ly/2gQkK>

Experientia © 2006 M. Vanderbeeken et al. <http://bit.ly/hetA0x>  
Second Life © 2003 – 2011 Linden Labs, Inc., <http://bit.ly/xbv0L>  
Image © 2006 Philips Design

We Are Arcade © 2011 D. Grossetti et al. <http://bit.ly/MALJU>  
World of Warcraft: Calcsys review © 2011  
J. Greer, <http://bit.ly/ENH0x>  
World of Warcraft © 2001 – 2011  
Blizzard Entertainment, Inc., <http://bit.ly/2gQkK>

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## Visualization [4]: Augmented Reality (AR)

- Augmented Reality: Computer-Generated (CG) Sensory Overlay**
- Added to Physical, Real-World Environment**

"40 Best Augmented Reality (iPhone Applications)", © 2010 iPhoneNews.com, <http://bit.ly/2gQkK>  
My Nav © 2010 Winfield & Co. <http://bit.ly/2gQkK>

Google goggles  
Wikipedia, Google Goggles: <http://bit.ly/3dX8E>

Bing Maps © 2010 – 2011  
Microsoft Corporation  
<http://bit.ly/3dX8E>  
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CIS 536/636 Introduction to Computer Graphics Lecture 23 of 43 Computing & Information Sciences Kansas State University



## Summary

- Reading for Last Class: §17.1 – 17.2, Eberly 2<sup>e</sup>
- Reading for Today: Chapter 10, 13, §17.3 – 17.5, Eberly 2<sup>e</sup>
- Reading for Next Class: §2.4.3, 8.1, Eberly 2<sup>e</sup>, **GL handout**
- Last Time: Rotations in Animation
  - \* Matrix, fixed angles, Euler angles, axis
  - \* Quaternions & how they work – properties, arithmetic operations
  - \* Gimbal lock defined & illustrated
- Quaternions Concluded
  - \* Incremental rotation: spherical linear interpolation (slerping)
  - \* Advantages of slerping vs. cubic interpolation between Euler angles
  - \* Uses: character animation, camera control (rotating Look vector)
- Dynamics & Kinematics (Preview of Lectures 28 – 30)
- Today: Modeling & Simulation
  - \* Virtual / augmented reality (VR/AR) & virtual environments (VE)
  - \* Visualization & simulation (Viz-Sim) preview



## Terminology

- Last Time: Rotation using **Matrices, Fixed Angles, Euler Angles**
- **Gimbal Lock**
  - \* Loss of DOF
  - \* Reference (© 2007 S. Seefeldt): <http://bit.ly/e1nuo9>
- **Axis-Angle** – Rotate Reference Vector  $r$  about Arbitrary Axis (Vector)  $A/n$
- **Quaternions**
  - \* Quaternions – different representation of arbitrary rotation
  - \* Exponential maps – 3-D representation related to quaternions
- **Visualization** – Communicating with Images, Diagrams, Animations
- **Simulation** – Artificial Model of Real Process for Answering Questions
- VR, VE, VA, AR
  - \* Virtual Reality: computer-simulated environments, objects
  - \* Virtual Environment: part of VR dealing with surroundings
  - \* Virtual Artifacts: part of VR dealing with simulated objects
  - \* Augmented Reality: CG sensory overlay on real-world images

